PPPL-5390

A nonlocal ion heat flux closure for antiparallel reconnection

J. Ng, A. Hakim, and A. Bhattacharjee

May 2017



Prepared for the U.S.Department of Energy under Contract DE-AC02-09CH11466.

Princeton Plasma Physics Laboratory Report Disclaimers

Full Legal Disclaimer

This report was prepared as an account of work sponsored by an agency of the United States Government. Neither the United States Government nor any agency thereof, nor any of their employees, nor any of their contractors, subcontractors or their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or any third party's use or the results of such use of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof or its contractors or subcontractors. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof.

Trademark Disclaimer

Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof or its contractors or subcontractors.

PPPL Report Availability

Princeton Plasma Physics Laboratory:

http://www.pppl.gov/techreports.cfm

Office of Scientific and Technical Information (OSTI):

http://www.osti.gov/scitech/

Related Links:

U.S. Department of Energy

U.S. Department of Energy Office of Science

U.S. Department of Energy Office of Fusion Energy Sciences

A nonlocal ion heat flux closure for antiparallel reconnection

Jonathan Ng, Ammar Hakim, and A. Bhattacharjee

Center for Heliophysics, Department of Astrophysical Sciences and Princeton Plasma Physics Laboratory,

Princeton University, Princeton, NJ 08543, USA

Adam Stanier and W. Daughton

Los Alamos National Laboratory, Los Alamos, NM 87545, USA

(Dated: May 2, 2017)

The integration of kinetic effects in fluid models is important for global simulations of the Earth's magnetosphere. In particular, it has been shown that ion kinetics play a crucial role in the dynamics of large reconnecting systems, and that higher-order fluid moment models can account for some of these effects. Here we introduce a ten-moment model for electrons and ions, which includes the off diagonal elements of the pressure tensor that are important for magnetic reconnection. Kinetic effects are recovered by introducing a nonlocal heat flux closure, which approximates linear Landau damping in the fluid framework. The closure is tested using the island coalescence problem, which is sensitive to ion dynamics. We demonstrate that the nonlocal closure is able to self-consistently reproduce the structure of the ion diffusion region, pressure tensor and ion velocity without the need for fine-tuning of relaxation coefficients present in earlier models.

Magnetic reconnection is a change in topology of the magnetic field lines in a plasma [1], often followed by the conversion of stored magnetic energy to the kinetic energy of accelerated particles. It is believed to play an important role in many laboratory and astrophysical plasma processes, including sawtooth crashes in tokamaks, solar flares, magnetic substorms in the Earth's magnetosphere and coronal mass ejections [2–6].

For reconnection to take place, the motion of the plasma must decouple from the magnetic field lines. In collisionless environments such as the magnetosphere, this takes place in the electron diffusion region, and due to the kinetic scales involved, cannot be described purely by resistive magnetohydrodynamic (MHD) models such as the Sweet-Parker model [7, 8]. For large scale global numerical studies of the magnetosphere, which are crucial for accurate space weather prediction, the use of fluid models is common due to the computational cost involved in simulating the large domains involved. Thus, the development of extended fluid models incorporating collisionless effects is desirable for capturing the physics of reconnection in large systems.

The major issue with fluid models is the closure of the hierarchy of fluid equations obtained by taking moments of the kinetic equation. While increasing the number of moments allows more information about the distribution function to be captured [9], a choice must be made as to when to close the equations and how to treat the highest moment. Most closures of the moment equations involve an expansion in small Knudsen number in the collisional regime, and attempts have been made to use these models to simulate magnetic reconnection [10–13].

However, in the collisionless case, kinetic effects such as phase mixing are present and cannot be captured by these fluid closures [14, 15]. Instead, approximations can be made by introducing collisionless damping coefficients by expressing the highest moments in terms of lower moments. Unlike the collisional case, the closure coefficients can be complex and are nonlocal in space [14, 15]. While these models have been used extensively in studies of fusion plasmas [16, 17], they have not been applied to studies of magnetic reconnection.

In this paper we describe the self-consistent implementation of a fluid closure using the ten-moment equation system without any adjustable parameters. We evolve the full pressure tensor for both electrons and ions, which is necessary to balance the reconnection electric field in collisionless reconnection [18, 19], and close for the heat flux using a three-dimensional extension of the Hammett-Perkins closure [14]. We perform simulations of the island coalescence problem, in which the existing Hall MHD fluid model does not reproduce the kinetic result due to the absence of important ion physics [20, 21]. We demonstrate here with the collisionless fluid model that the wider ion diffusion region can be reproduced without the fine tuning of a free parameter as was previously required [21]. While the strong system-size scaling of the reconnection rate in kinetic and hybrid (kinetic ion, fluid electron) simulations is not completely reproduced for larger scales, the new closure successfully captures the ion-scale structures such as agyrotropy which are not accounted for consistently by earlier fluid models.

The ten-moment equations are derived by taking moments of the kinetic equation

$$\frac{\partial n}{\partial t} + \frac{\partial}{\partial x_j} (nu_j) = 0$$

$$m \frac{\partial}{\partial t} (nu_i) + \frac{\partial \mathcal{P}_{ij}}{\partial x_j} = nq(E_j + \epsilon_{ijk}u_j B_k). \tag{1}$$

$$\frac{\partial \mathcal{P}_{ij}}{\partial t} + \frac{\partial \mathcal{Q}_{ijk}}{\partial x_k} = nqu_{[i}E_{j]} + \frac{q}{m}\epsilon_{[ikl}\mathcal{P}_{kj]}B_l,$$

where \mathcal{P}_{ij} and \mathcal{Q}_{ijk} are the second and third moments of

the distribution function

$$\mathcal{P}_{ij} \equiv m \int v_i v_j f d^3 v$$

$$\mathcal{Q}_{ijk} \equiv m \int v_i v_j v_k f d^3 v,$$
(2)

and the square brackets denote a sum over permutations of the indices (e.g. $u_{[i}E_{j]} = u_iE_j + u_jE_i$). The third moment tensor Q_{ijk} can be written in terms of the heat flux tensor $q_{ijk} \equiv m \int (v_i - u_i)(v_j - u_j)(v_k - u_k)fd^3v$

$$\mathcal{Q}_{ijk} = q_{ijk} + u_{[i}\mathcal{P}_{jk]} - 2mnu_iu_ju_k.$$
(3)

Earlier multi-fluid models of reconnection involving a pressure tensor have employed a relaxation to local isotropy in the form $\partial_i q_{ijk} = nv_t |k_0| (T_{ij} - T_0 \delta_{ij})$. Here $v_t = \sqrt{2T/m}$ is the thermal velocity of the associated species and k_0 is a free parameter which effectively allows deviations from isotropy at length scales less than $1/|k_0|$ [10, 11, 13, 21]. It has been shown that simulation results are sensitive to the choice of k_0 for each species [13, 21] and such free parameters are present in earlier efforts as well [10, 11, 13].

In order to close the equations in the collisionless limit, we use a three-dimensional extension of the Hammett-Perkins closure, which can be expressed as follows for both electrons and ions [14]:

$$q_{ijk}(\mathbf{x}) = n(\mathbf{x})\hat{q}_{ijk}(\mathbf{x}) \tag{4}$$

where \hat{q}_{ijk} in Fourier space is \tilde{q}_{ijk} and is calculated as

$$\tilde{q}_{ijk} = -i \frac{v_{\iota}}{|k|} \chi k_{[i} \tilde{T}_{jk]}.$$
(5)

Here T_{jk} is the Fourier transform of the deviation of the local temperature tensor from the mean. The 1/|k| scaling makes this a non-local closure when expressed in real space [15, 16] and provides a 1 to 3 pole Padé approximation of various components of the dielectric tensor. The coefficient $\chi = \sqrt{4/9\pi}$ is the best fit value for the diagonal q_{iii} component and reduces to the closure in Refs. [14, 15] in the 1-D limit. This is an unmagnetised closure (especially relevant to ions in this geometry in which there is no guide field) which approximates linear phase mixing, allowing the wavenumber-dependent damping of spurious short-wavelength oscillations which are present in higher moment fluid models [15, 22], and to our knowledge, is the first of its kind in closure studies of magnetic reconnection.

The moment equations coupled to Maxwell's equations are implemented in the finite-volume version of the Gkeyll code, which uses a high-resolution wave propagation method for the hyperbolic part of the equations and a point implicit method for the source terms [23, 24]. The closure is evaluated using an interface to the parallel FFTW library [25].



FIG. 1. (a) Damping of electrostatic fluctuations in 1-D tenmoment simulations. (b) Reconnection rates in kinetic, tenmoment and Hall MHD simulations. (c) Scaling of maximum reconnection rate with system size. (d) Scaling of average reconnection rate over $1.5t_A$ with system size.

We first illustrate the effects of the closure in Fig. 1(a). which shows the evolution of the electric field amplitude for a Langmuir wave with $k\lambda_{de} = 0.35$ in a 1-D twofluid simulation, where λ_{de} is the electron Debye length. In the simulation, the measured frequency and damping rate in terms of the electron plasma frequency ω_{pe} are $\omega = 1.16\omega_{pe}$, $\gamma = 0.044\omega_{pe}$ respectively, compared to the exact solution from the linear Vlasov dispersion relation $\omega = 1.22\omega_{pe}$, $\gamma = 0.034\omega_{pe}$. Here we note that the measured values are consistent with those calculated using the Padé approximant of the plasma dispersion function, and improved agreement with the Vlasov solution requires evolving higher fluid moments [14–16]. In contrast, the simulation without any explicit dissipation is qualitatively different and shows no damping as expected.

For magnetic reconnection, while the Harris sheet geometry is a standard test problem [26], and has been successfully simulated using this closure (not shown), we focus on the island coalescence geometry in this paper as it has been found to be sensitive to ion rather than electron dynamics [20, 21], where for which this closure would be a better approximation. This is a Fadeev equilibrium with initial conditions [27]

$$A_y = -\lambda B_0 \ln \left[\cosh(z/\lambda) + \epsilon \cos(x/\lambda) \right]$$

$$n = n_0 (1 - \epsilon^2) / \left[\cosh(z/\lambda) + \epsilon \cos(x/\lambda) \right]^2 + n_b.$$
(6)

Here B_0 is the x-component of the magnetic field upstream of the layer, ϵ controls the island size and λ is the half width of the current sheet. We use the same physical parameters as described in previous studies [20, 21, 28], with $\epsilon = 0.4$, which corresponds to an island half-width of approximately 1.2λ , and background density $n_b = 0.2n_0$. The system size is $L_x \times L_z = 4\pi\lambda \times 2\pi\lambda$, with periodic boundary conditions in the x direction. Conducting walls for fields and reflecting walls for particles are used in the z direction. We use mass ratio $m_i/m_e = 25$, electron thermal speed $v_{t,e}/c = 0.35$ and $T_i = T_e = T$, and the value of T is set by the upstream equilibrium condition $\beta = 1$. The ratio of electron plasma frequency to gyrofrequency is $\omega_{pe}/\Omega_{ce} = 2$. A 10% initial perturbation in the magnetic field is applied to initiate merging. The kinetic results in this paper are described in Ref. [20] and additional simulations for the $\lambda/d_i = 5$, 10 cases were performed using the particle-in-cell code PSC [29].

In MHD, multi-fluid and kinetic models, the initial phase in which the islands approach each other is driven by the ideal MHD coalescence instability [30], and differences between the models only appear after the central current sheet begins to form [20, 21]. This can be seen in Fig. 1(b), which shows the normalised reconnection rate for simulations using the new closure and comparisons to earlier kinetic, ten-moment and Hall MHD simulations [20, 21]. Here the reconnection rate is $E_R = (1/B'V'_A)\partial\psi/\partial t$ in the same manner as in Refs.[20, 21, 28], where B' and V'_A are calculated using the maximum magnetic field between the centres of the two islands at t = 0. The flux within an island ψ is defined as the difference between A_y at the X- and Opoints.

Because reconnection in this system is bursty, it is useful to consider the average as well as maximum reconnection rates [20, 21, 28]. In Figs. 1(c-d), the scaling of the maximum and average (over 1.5 global Alfvén times) reconnection rates with system size is shown. With the nonlocal closure, there is a stronger negative scaling of the average reconnection rate $\propto (\lambda/d_i)^{-0.45}$ for system sizes up to $\lambda/d_i = 25$ compared to $(\lambda/d_i)^{-0.2}$ for both Hall MHD and ten moment simulations with a local closure. However, this is still weaker than the results of Ref. [20] where the rate scales like $\propto (\lambda/d_i)^{-0.8}$ and $(\lambda/d_i)^{-0.65}$ for kinetic and hybrid models respectively. The discrepancies for the ten moment systems are partially explained by the enhancement of the reconnection rate due to the formation of secondary islands in smaller systems $(\lambda/d_i = 15$ for the nonlocal closure, $\lambda/d_i = 25$ for the local closure).

Figure 2 shows a comparison between the kinetic, tenmoment and Hall MHD simulations with $\lambda = 5d_i$ at $t = t_A$, which is close to the time of maximum reconnection rate. As can be seen in the bottom panel, the width of the current sheet in the ten-moment simulation is comparable to that in the kinetic simulation (1.20 d_i vs 1.15 d_i), and is much larger than the highly peaked Hall MHD current sheet (0.18 d_i). The peak current density is still higher than in the kinetic simulation due to the electron dynamics in the ten-moment model, which causes a more intense electron layer due to the isotropisation



FIG. 2. Current densities in kinetic, ten-moment and Hall MHD simulations with $\lambda = 5d_i$. The colour scaling of the Hall MHD current is reduced by a factor of two so the strongly peaked current sheet can be seen.



FIG. 3. Comparison of the decomposition of the ion momentum equation near the x-point between the nonlocal tenmoment model and a kinetic simulation.

of the pressure tensor. Here the electron closure captures the off-diagonal terms of the pressure tensor which balance the reconnection electric field in the electron diffusion region self-consistently, but produces weaker electron pressure anisotropy than models which focus on particle trapping effects [31–33]; this does not affect the results of this paper as the reconnection rates are sensitive to the ion dynamics for this geometry [20, 21].

The structure of the ion diffusion region is shown in Fig. 3, which contains the decomposition of the ion momentum equation on a cut along z = 0 at $t = t_A$. In Ref. [20] it was shown that the influence of the ion kinetic physics extends to a broader 2-3 d_i ion diffusion

region, where the divergence of the pressure tensor balances the non-ideal electric field. This result is in contrast to the Hall MHD result, where the ion inertia balances the reconnection electric field below d_i scales [20].

While both local and nonlocal ten-moment models could capture the wider ion diffusion region, it was found that keeping the relaxation parameter $k_i = 1/d_e$, which was used in the Harris sheet study [13], caused larger Hall MHD-like reconnection rates to be observed and a narrower ion diffusion region to form. Only by adjusting k_i in the ion closure to $1/(3d_i)$, allowing the pressure tensor to deviate from isotropy at larger scales, could the kinetic reconnection rates be reproduced for small systems [21].

In contrast, with the nonlocal closure, the wider ion diffusion region develops self-consistently without the need to fine tune the relaxation. While the reconnection rate does not match the kinetic result exactly, the larger region in which the divergence of the ion pressure tensor balances the non-ideal electric field is reproduced, with the associated reduction of the reconnection rate as compared to that of Hall MHD or the local ten-moment model with larger k_i [21].

Additionally, due to the wavenumber-dependent damping, the model using the nonlocal closure shows good agreement in the ion velocity with the kinetic results, apart from the absence of PIC noise. This is because the new closure does not exhibit some of the spurious structures which have been observed when using the local closure. These are most evident along the line x = 0, where the ion velocity is reduced, and just upstream of the reconnection region in Fig. 4. The structures are present with the local closure due to the lower k_i used to obtain the wider diffusion region, which does not account for the faster damping at shorter wavelengths, unlike the nonlocal closure, which approximates this effect.

Further improvements when using the nonlocal closure are illustrated by considering a common metric used in reconnection, the agyrotropy $A\emptyset$, which measures the departure of the distribution function from cylindrical symmetry [34]. Figure 5 shows the ion agyrotropy $A\emptyset_i$ observed close to the central current sheet at $t = t_A$. In the kinetic simulation, there is strong agyrotropy in both a 2-3 d_i thick region upstream of the current sheet and the exhaust region and it was shown in Ref. [20] that this corresponds to the region where ion motion is characterised by meandering orbits and ion pressure tensor effects contribute to momentum balance.

With the new nonlocal closure shown in the second panel of Fig. 5, the structure of the agyrotropy both upand downstream of the x-point is reproduced. This is a qualitative improvement on the local model, which shows two distinct upstream regions and small agyrotropy in the exhaust region. The improvement is due to the nonlocal heat flux, which reduces the discrepancies in the diagonal components of the ion pressure tensor observed



FIG. 4. Out-of-plane ion velocity in kinetic, nonlocal fluid and local fluid models. The local model uses $k_i = 1/(3d_i)$ which was chosen to match reconnection rates with the kinetic solution in Ref. [20].



FIG. 5. Comparison of ion agyrotropy between kinetic, nonlocal fluid and local fluid models. The local model uses $k_i = 1/(3d_i)$ which was chosen to match reconnection rates with the kinetic solution in Ref. [20].

when only using the local model [12]. However, the values of the agyrotropy using the nonlocal closure are still lower than the kinetic results, as the fluid model cannot capture all the details of the non-gyrotropic distribution function caused by the meandering motion.

To summarise, we have implemented a nonlocal ion closure for the two-fluid, ten-moment equations that captures linear phase mixing in a fluid treatment. This provides heat flux at the x-point which is necessary for reconnection to take place in the collisionless ten moment model [12]. We demonstrate that using the new nonlocal closure gives improved agreement with kinetic results compared to previously implemented systems for moment closures and Hall MHD [13, 21], by allowing the ion pressure tensor to deviate from isotropy without introducing a free relaxation parameter. This sets the structure of the ion diffusion region self-consistently, and results in much improved agreement highlighted by the ion velocity profile and agyrotropy. However, the strong system-size dependence of the average reconnection rate observed in kinetic and hybrid simulations is not completely reproduced [20]. The scaling is due in part to the formation of secondary islands in the larger fluid systems, and also indicates that while the ion diffusion region physics is reproduced, there is still additional ion kinetic physics, such as the ion meandering motion and its effects on the distribution function [20], that contributes to setting the reconnection rate in this system. While this system is less sensitive to the electron dynamics [20, 21], the nonlocal closure is also able to capture the off diagonal terms of the electron pressure tensor in the electron diffusion region. Future work could explore the extension to the strongly magnetised regime in a similar manner [15, 35], which could allow the treatment of guide-field reconnection and application to large systems, in which the development of strong electron pressure anisotropy is also an important process [32, 33].

This work was supported by NSF Grants AGS-0962698, AGS-1338944, DOE Contract DE-AC02-09CH11466 and NASA Grant NNH13AW51I. This research used resources of the National Energy Research Scientific Computing Center, a DOE Office of Science User Facility supported by the Office of Science of the U.S. Department of Energy under Contract No. DE-AC02-05CH11231 and Trillian, a Cray XE6m-200 supercomputer at UNH supported by the NSF MRI program under grant PHY-1229408. We thank G. Hammett for fruitful discussions.

- [1] J. Dungey, Philosophical Magazine Series 7 44, 725 (1953).
- [2] S. von Goeler, W. Stodiek, and N. Sauthoff, Phys. Rev. Lett. 33, 1201 (1974).
- [3] V. M. Vasyliunas, Reviews of Geophysics 13, 303 (1975).
- [4] T. D. Phan, L. M. Kistler, B. Klecker, G. Haerendel, G. Paschmann, B. U. O. Sonnerup, W. Baumjohann, M. B. Bavassano-Cattaneo, C. W. Carlson, A. M. Dilellis, K. H. Fornacon, L. A. Frank, M. Fujimoto, E. Georgescu, S. Kokubun, E. Moebius, T. Mukai, M. Oieroset, W. R. Paterson, and H. Reme, Nature 404, 848 (2000).
- [5] A. Bhattacharjee, Z. W. Ma, and X. Wang, Physics of Plasmas 8, 1829 (2001).
- [6] M. Yamada, R. Kulsrud, and H. Ji, Rev. Mod. Phys. 82, 603 (2010).
- [7] P. A. Sweet, in Electromagnetic phenomena in cosmic physics [34] J. Scudder and W. Daughton, Journal of Geophysical Vol. 6 (1958) pp. 123-134.
- [8] E. N. Parker, Journal of Geophysical Research 62, 509 (1957).

- [9] H. Grad, Communications on Pure and Applied Mathematics 2, 331 (1949).
- [10] M. Hesse, D. Winske, and M. M. Kuznetsova, Journal of Geophysical Research: Space Physics 100, 21815 (1995).
- [11] L. Yin, D. Winske, S. P. Gary, and J. Birn, Journal of Geophysical Research: Space Physics ${\bf 106},\, 10761$ (2001).
- [12] E. A. Johnson, Ph.D. thesis, University of Wisconsin-Madison (2011).
- [13] L. Wang, A. H. Hakim, A. Bhattacharjee, and K. Germaschewski, Physics of Plasmas (1994-present) 22, 012108 (2015).
- [14] G. W. Hammett and F. W. Perkins, Phys. Rev. Lett. 64, 3019 (1990).
- [15] G. W. Hammett, W. Dorland, and F. W. Perkins, Physics of Fluids B 4, 2052 (1992).
- [16] P. B. Snyder and G. W. Hammett, Physics of Plasmas 8, 3199 (2001).
- [17] X. Q. Xu, P. W. Xi, A. Dimits, I. Joseph, M. V. Umansky, T. Y. Xia, B. Gui, S. S. Kim, G. Y. Park, T. Rhee, H. Jhang, P. H. Diamond, B. Dudson, and P. B. Snyder, Physics of Plasmas 20, 056113 (2013), http://dx.doi.org/10.1063/1.4801746.
- [18] A. Ishizawa, R. Horiuchi, and H. Ohtani, Physics of Plasmas 11, 3579 (2004).
- [19] M. Hesse, S. Zenitani, and A. Klimas, Physics of Plasmas 15, 112102 (2008), http://dx.doi.org/10.1063/1.3006341.
- [20] A. Stanier, W. Daughton, L. Chacón, H. Karimabadi, J. Ng, Y.-M. Huang, A. Hakim, and A. Bhattacharjee, Phys. Rev. Lett. 115, 175004 (2015).
- [21] J. Ng, Y.-M. Huang, A. Hakim, A. Bhattacharjee, A. Stanier, W. Daughton, L. Wang, and K. Germaschewski, Physics of Plasmas 22, 112104 (2015).
- [22] P. J. Palmadesso, S. B. Ganguli, and H. G. Mitchell, "Multimoment fluid simulations of transport processes in the auroral zones," in Modeling Magnetospheric Plasma (American Geophysical Union, 1988) pp. 133-143.
- [23] A. Hakim, J. Loverich, and U. Shumlak, Journal of Computational Physics 219, 418 (2006).
- [24] A. Hakim, Journal of Fusion Energy 27, 36 (2008).
- [25] M. Frigo and S. G. Johnson, Proceedings of the IEEE 93, 216 (2005), special issue on "Program Generation, Optimization, and Platform Adaptation".
- [26] E. Harris, Il Nuovo Cimento (1955-1965) 23, 115 (1962), 10.1007/BF02733547.
- [27] V. M. Fadeev, I. F. Kvartskhava, and N. N. Komarov, Nucl. Fusion 5 (1965).
- [28] H. Karimabadi, J. Dorelli, V. Roytershteyn, W. Daughton, and L. Chacón, Phys. Rev. Lett. 107, 025002 (2011).
- [29] K. Germaschewski, W. Fox, S. Abbott, N. Ahmadi, K. Maynard, L. Wang, H. Ruhl, and A. Bhattacharjee, Journal of Computational Physics 318, 305 (2016).
- [30] J. M. Finn and P. K. Kaw, Physics of Fluids 20, 72 (1977).
- [31] A. Le, J. Egedal, W. Daughton, W. Fox, and N. Katz, Phys. Rev. Lett 102, 085001 (2009).
- [32] O. Ohia, J. Egedal, V. S. Lukin, W. Daughton, and A. Le, Phys. Rev. Lett. 109, 115004 (2012).
- [33] J. Egedal, A. Le, and W. Daughton, Physics of Plasmas 20, 061201 (2013).
- Research: Space Physics 113, n/a (2008), a06222.
- and P. L. Sulem, [35] P. Goswami, T. Passot, Plasmas Physics of 12, 102109(2005),

6



Princeton Plasma Physics Laboratory Office of Reports and Publications

Managed by Princeton University

under contract with the U.S. Department of Energy (DE-AC02-09CH11466)

P.O. Box 451, Princeton, NJ 08543 Phone: 609-243-2245 Fax: 609-243-2751 E-mail: publications@pppl.gov Website: http://www.pppl.gov