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## Ion Temperature Effects on Magnetotail Alfvén Wave Propagation and Electron Energization

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**Abstract.**

A new 2D self-consistent hybrid gyrofluid-kinetic electron model in dipolar coordinates is presented and used to simulate dispersive scale Alfvén wave pulse propagation from the equator to the ionosphere along an  $L = 10$  magnetic field line. The model is an extension of the hybrid MHD-kinetic electron model [*Damiano et al.*, 2007] that incorporates ion Larmor radius corrections via the kinetic fluid model of *Cheng and Johnson* [1999]. It is found that consideration of a realistic ion to electron temperature ratio decreases the propagation time of the wave from the plasma sheet to the ionosphere by several seconds relative to a  $\rho_i = 0$  case (which also implies shorter timing for a substorm onset signal) and leads to significant dispersion of wave energy perpendicular to the ambient magnetic field. Additionally, ion temperature effects reduce the parallel current and electron energization all along the field line for the same magnitude perpendicular electric field perturbation.

## 1. Introduction

20 The formation of the broadband aurora, which are seen to increase rapidly at substorm  
 21 onset [e.g. *Wing et al.*, 2013], have been linked to electron precipitation associated with  
 22 dispersive scale Alfvén waves - waves with perpendicular scale lengths on the order of  $\lambda_e$ ,  
 23  $\rho_s$  and  $\rho_i$  [*Keiling et al.*, 2003]. How electrons interact with these waves is dictated by the  
 24 location of the wave along the field line. Close to the ionospheric boundary,  $\beta \ll m_e/m_i$ ,  
 25 electron inertial effects dominate and electrons can be energized by Fermi acceleration  
 26 processes [e.g. *Kletzing*, 1994; *Chaston et al.*, 2000; *Watt and Rankin*, 2009]. Toward the  
 27 plasma sheet, waves are in the kinetic Alfvén wave regime ( $\beta \gg m_e/m_i$ ) and can couple  
 28 to electrons which have parallel velocities close to the phase speed of the wave [e.g. *Watt*  
 29 *and Rankin*, 2009]. In this latter region, ion gyroradius effects are expected to play an  
 30 important role because in the plasma sheet  $T_i/T_e \sim 7$  [*Baumjohann et al.*, 1989] which  
 31 implies that  $\rho_i$  effects will control the phase speed of the wave, which affects both the  
 32 propagation time of the wave from an onset site to the ionosphere [e.g. *Lessard et al.*,  
 33 2006; *Chi et al.*, 2009] and the resonance condition necessary for electron acceleration.  
 34 Additionally,  $\rho_i$  is an important scale length associated with the cross scale coupling of  
 35 wave energy to kinetic scales through a turbulent cascade [*Chaston et al.*, 2008].

36 Although there is a significant body of previous simulation work devoted to electron  
 37 acceleration by dispersive scale waves [*Kletzing*, 1994; *Chaston et al.*, 2000; *Chaston et al.*,  
 38 2002; *Watt et al.*, 2004; *Damiano and Wright*, 2005; *Watt et al.*, 2006; *Watt and Rankin*,  
 39 2009] attention to ion gyroradius effects has been relatively limited to studies involving  
 40 gyrofluid approaches without self consistent coupling to kinetic electrons (e.g. *Su et al.*

41 [2006] and *Jones and Su* [2008], in application to Jovian aurora, and *Streltsov et al.* [1998]  
 42 in application to terrestrial Field Line Resonances) or Particle-In-Cell treatments [*Shay*  
 43 *et al.*, 2011] that, although considering all the relevant physics, are restricted to more  
 44 localized studies in the plasma sheet due to the computational costs of considering the  
 45 full orbital dynamics of all the particles.

46 With this motivation in mind, we have adapted a 2D hybrid MHD-kinetic electron  
 47 model in curvilinear coordinates [*Damiano et al.*, 2007; *Damiano and Wright*, 2008],  
 48 which has been used extensively to consider electron acceleration in geomagnetic Field  
 49 Line Resonances, to include ion gyroradius effects using the kinetic-fluid model of *Cheng*  
 50 *and Johnson* [1999]. The model is used to simulate kinetic Alfvén wave propagation from  
 51 an equatorial source region in the magnetotail (where these waves are ubiquitous within  
 52 about  $15 R_E$ , associated with the breaking of reconnection induced fast flows - *Chaston*  
 53 *et al.* [2012]) to the ionospheric boundary of the simulation domain. The rest of the paper  
 54 is broken up into four sections. Section 2 summarizes the hybrid model used. Section 3  
 55 presents the simulation results while Section 4 gives our conclusions.

## 2. Gyrofluid-Kinetic-Electron Model

56 The simulations were conducted with the new 2-D Gyrofluid-Kinetic Electron (GKE)  
 57 model in dipolar coordinates, which is the gyrofluid extension of the hybrid MHD-kinetic  
 58 electron model [*Damiano et al.*, 2007] that has been used primarily to date to investigate  
 59 electron dynamics in geomagnetic Field Line Resonances [*Damiano et al.*, 2007; *Damiano*  
 60 *and Wright*, 2008; *Damiano and Johnson*, 2012]. The model treats electron motion along  
 61 field lines as drift-kinetic, and ions with a kinetic-fluid closure based on a solution of the  
 62 linear gyrokinetic equation [*Cheng and Johnson*, 1999], which includes ion Larmor radius

corrections as well as the physics of the ion polarization current. The model geometry is illustrated in Figure 1a and explicitly includes the field aligned direction ( $x_1$ ) and the direction across L shells ( $x_2$ ). The system is independent of the azimuthal coordinate so that  $\partial/\partial x_3 = 0$ . In denoting the component electron velocities we will also use the notation  $v_{||} = v_1$  and  $v_{\perp} = \sqrt{v_2^2 + v_3^2}$  to indicate the gyrophase independent perpendicular velocity.

Consistent with the Field Line Resonance studies presented in *Damiano and Wright* [2008] and *Damiano and Johnson* [2012, 2013], the simulation grid used in this analysis is 0.6  $R_E$  wide at the equator and the ionospheric boundaries are set to a geocentric altitude of 2  $R_E$ . This altitude corresponds to the average location of the  $B/n$  peak (where the peak electron acceleration is believed to occur [*Wright et al.*, 2002; *Damiano and Wright*, 2008]) and the width of the grid tapers down to about 100 km at this altitude [*Damiano and Johnson*, 2013]. In this topology, the perpendicular scale lengths of the kinetic Alfvén waves imposed at the equator (as discussed later in the section), naturally taper down to electron inertial scales close to the ionospheric boundary.

The gyrofluid portion of the model incorporates the modified linearized momentum equation given by

$$\mu_o \rho_o \frac{\partial \tilde{u}_3}{\partial t} = \frac{B_o}{h_1 h_3} \left( \frac{\partial}{\partial x_1} (h_3 b_3) \right) \quad (1)$$

where the ion gyroradius ( $\rho_i$ ) response is included via the perpendicular pressure term which can be expressed in the form of a modified velocity given by  $\tilde{u}_3 = (1 - 1.25 \rho_i^2 \nabla_{\perp}^2) u_3$ . The coefficients of  $\rho_i^2 \nabla_{\perp}^2$  here are obtained using a Padé approximation [*Johnson and Cheng*, 1997; *Cheng and Johnson*, 1999]. This equation is coupled to Faraday's law

$$\frac{\partial b_3}{\partial t} = \frac{-1}{h_1 h_2} \left( \frac{\partial}{\partial x_1} (h_2 E_2) - \frac{\partial}{\partial x_2} (h_1 E_1) \right) \quad (2)$$

and the perpendicular (where Padé approximants have also been used)

$$E_2 = -B_o(1 - \rho_i^2 \nabla_\perp^2) \tilde{u}_3 \quad (3)$$

and parallel Ohm's laws

$$\begin{aligned} \frac{\partial}{\partial x_2} \left( \frac{h_3}{h_1 h_2} \left( \frac{\partial h_1 E_1}{\partial x_2} \right) \right) - \frac{h_1 E_1}{\lambda_e^2} &= \frac{\partial}{\partial x_2} \left( \frac{h_3}{h_1 h_2} \frac{\partial}{\partial x_1} (h_2 E_2) \right) \\ &+ e \mu_o \frac{\partial}{\partial x_1} \int v_1^2 f d^3 v \\ &+ \mu_o \frac{e}{m_e} \frac{\partial B_o}{\partial x_1} \int \mu_m f d^3 v \\ &- 2 \mu_o \frac{e}{m_e} \frac{\partial B_o}{\partial x_1} \int \frac{m_e v_1^2}{2 B_o} f d^3 v \end{aligned} \quad (4)$$

where  $x_1 = \cos \theta / r^2$ ,  $x_2 = \sin^2 \theta / r$ ,  $x_3 = \phi$ ,  $h_1 = r^3 / (1 + 3 \cos^2 \theta)^{1/2}$ ,  $h_2 = r^2 / (\sin \theta (1 + 3 \cos^2 \theta)^{1/2})$ , and  $h_3 = r \sin \theta$ . A similar gyrofluid closure was also used in the two fluid model of *Streltsov et al.* [1998]. In equation (4),  $\lambda_e = \sqrt{m_e / \mu_o n e^2}$  is the electron inertial length,  $\mu_m = m_e v_\perp^2 / (2B)$  is the electron magnetic moment, the second term on the right hand side relates to the parallel gradient of the electron pressure while the third and fourth terms incorporate the perpendicular and parallel electron pressures.

Parallel electron dynamics are described by the guiding center equations

$$m_e \frac{dv_1}{dt} = -e E_1 - \mu_m \frac{1}{h_1} \frac{\partial B_o}{\partial x_1} \quad (5)$$



$$h_1 \frac{dx_1}{dt} = v_1 \quad (6)$$

where  $v_1 = v_{\parallel}$  is the parallel electron velocity and the integral moments of the electron distribution function used in the parallel Ohm's law are computationally treated as summations using standard Particle-In-Cell techniques as discussed in *Damiano et al.* [2007].

For the present simulations, electrons are initially positioned to form a constant density such that  $n_e = n_i = 1 \text{ cm}^{-3}$  (which yields  $\lambda_e \approx 5 \text{ km}$ ) and a uniform electron distribution is assumed in velocity space. Perfectly conducting boundary conditions are assumed at the ionospheres, while at the perpendicular boundaries (along the lines of constant  $x_2$ ) a node in current is imposed.

Equations (1) to (3) with  $E_1 = 0$  are a self-consistent set of equations which incorporates ion gyroradius effects on Alfvén wave propagation, but neglects kinetic electron physics. In a cartesian geometry with uniform plasma parameters, these equations, along with a parallel momentum equation including electron temperature effects, yield a dispersion relation of the form:

$$\omega = k_{\parallel} V_A \sqrt{1 + k_{\perp}^2 \rho_i^2 \left(1 + \frac{T_e}{T_i}\right)} \quad (7)$$

where, as a result of the use of Padé approximants [e.g. see *Johnson and Cheng*, 1997; *Streltsov et al.*, 1998; *Cheng and Johnson*, 1999], this expression provides a uniform approximation to the analytical dispersion relation [e.g. see *Hasegawa*, 1976; *Lysak and Lotko*, 1996] on all scales to within an accuracy of 6% [*Streltsov et al.*, 1998]. As such, it

is preferable to the commonly used small or large scale expansions and will be used in the analysis of the some of the simulation data to follow.

Waves are launched by a perturbation of azimuthal velocity, applied at  $t=0$ , which corresponds to the initial perpendicular electric field shown in Figure 1b. This is equivalent to perturbing the ion polarization current. The amplitude of the  $E_2$  profile is chosen to be order of magnitude comparable with observations [e.g. *Keiling, 2009*] and the wave perturbation is centered in the equatorial plane, where we assume a parallel Gaussian profile with a Full-Width-Half Max of  $1 R_E$  and a perpendicular scale length (for a majority of this study) of  $0.1 R_E$  (which yields  $k_\perp \rho_i \sim 1$  for  $T_i = 1$  keV and the resulting ratio  $k_\perp/k_\parallel \sim 10$  is within the range evident in the observations of *Chaston et al. [2014]*). This perturbation results in identical Alfvén wave pulses propagating toward the opposing ionospheric boundaries (with both upward and downward parallel current characteristics). For the purposes of this study, we focus on the pulse propagating toward the northern ionosphere (upper half plane of Figure 1a) carrying an upward directed field aligned current (along the field line denoted by the dotted line in the Figure 1b).

### 3. Simulations

The electron distribution function is initialized with a temperature of 100 eV, and we assume an ambient ion temperature of 1 keV which yields the field aligned profile of  $\rho_i$  displayed in Figure 2a. The resulting ratio of  $T_e/T_i = 1/10$  is roughly consistent with the average temperature ratio of  $1/7$  measured in the plasma sheet [e.g. *Baumjohann et al., 1989*]. Figure 2b illustrates the field-aligned Alfvén velocity profile and the horizontal line  $v_{th} = V_A$  (where  $v_{th} = \sqrt{2T_e/m_e}$ ) denotes the transition between the kinetic (KAW) and inertial (IAW) Alfvén wave regimes along the field line.

132 In order to make a consistent comparison between the  $T_i = 0$  ( $\rho_i = 0$ ) and the  $T_i = 1$  keV  
 133 cases, we initialized both systems so that the profiles and magnitudes of the perpendicular  
 134 electric field,  $E_2$ , were consistent. The pulse profile in the  $T_i = 1$  keV case is moving with  
 135 a higher speed and also has a reduced amplitude relative to the  $T_i = 0$  case. In Figure 3b,  
 136 the equatorial perpendicular scale length has been reduced to  $0.05 R_E$  (further increasing  
 137  $k_\perp \rho_i$ ) and the wave phase speed is further increased and the current amplitude further  
 138 reduced when compared to Figure 3a and the  $T_i = 0$  case.

139 The increased phase speed is in agreement with what would be expected from the  
 140 kinetic Alfvén wave dispersion relation, which (neglecting electron inertial effects) is given  
 141 by equation 7. Since,  $T_e \ll T_i$ , we can ignore the last term in the brackets, and since  
 142  $\lambda_\perp \sim 0.1 R_E$  and  $\rho_i \sim 100$  km at the equator,  $k_\perp \rho_i = 2\pi \rho_i / \lambda_\perp \sim 1$  and the dispersion  
 143 relation reduces to  $\omega / k_\parallel \sim \sqrt{2} V_A$ . As  $\rho_i$  and  $\lambda_\perp$  do not vary substantially between  
 144 the equator and  $l_\parallel = 1.5 R_E$ , this difference in velocity is roughly consistent with the  
 145 different propagation distances evident between the two cases in Figure 3a given the same  
 146 propagation times.

147 The reduction in the parallel current density between the cases displayed in Figure 3  
 148 can be understood from the cartoon inset in Figure 3b. The large gyroradius associated  
 149 with a hot ion temperature will, see a reduced orbit averaged perpendicular electric field  
 150 [*Tatsuno et al.*, 2009] and will consequently experience a reduced  $\langle \vec{E} \rangle \times \vec{B}$  drift and  
 151 polarization current relative to a cold ion with a gyroradius close to the perpendicular  
 152 scale length of the wave perturbation. The reduced polarization current associated with  
 153 the hot ion will consequently need to be closed by a reduced parallel current (and hence  
 154 a reduced  $E_\parallel$  to accelerate electrons). Essentially, hot ions do not respond to the field as

easily and this system must be driven harder to yield a similar parallel current relative to the  $T_i = 0$  case.

The reduction of  $E_{||}$  can also be seen from a linear analysis of the two fluid equations where the ratio of the parallel and perpendicular electric fields in the limit of the kinetic Alfvén wave is approximated by the expression [e.g. *Chaston et al.*, 2003; *Streltsov et al.*, 1998]

$$E_{||}/E_{\perp} = \frac{-k_{||}k_{\perp}\rho_s^2}{(1 + k_{\perp}^2\rho_i^2)} \quad (8)$$

and for a finite electron temperature, this ratio decreases with increase in the size of the ion gyrodisk (or increase in  $T_i$ ). The corresponding reduction of  $j_{||}$  can also be inferred from the equivalent expression for  $E_{\perp}/b_{\perp}$  (e.g. equation (48) of *Stasiewicz et al.* [2000]). Also consistent with this analytical description, the magnitude of  $E_{||}$  was significantly reduced in the high-altitude, near-equatorial plasma sheet region in two fluid simulations of Field Line Resonances when  $\rho_i$  effects were considered [*Streltsov et al.*, 1998].

The different phase speeds of the waves in the two cases considered, implies that we must superimpose the results at two different times in order to compare the evolution of the electron distribution function. Figure 4a super-imposes the profiles of the two runs so that the current maxima are centered at  $l_{||} = 5 R_E$ , and Figures 4b and 4c respectively illustrate the corresponding electron distribution function measured at the same location. In Figure 4b, at low energies, the initialized distribution has evolved to become elongated in the parallel direction at lower energies while maintaining the symmetry of the original Maxwellian distribution at higher energies. These characteristics of the distribution function are qualitatively consistent with what is evident in both observations [e.g. *Wygant*

176 *et al.*, 2002; *Janhunen et al.*, 2004] and simulations [e.g. *Watt and Rankin*, 2009, 2012].  
 177 As with *Watt and Rankin* [2009, 2012], when the driving electric field is increased, the  
 178 parallel asymmetry increases. However, in contrast to these other simulation efforts, we  
 179 have not time averaged the distribution function to better correspond to the observations  
 180 and we have used only a single pulse perturbation rather than the wave train that was  
 181 considered in the studies of *Watt and Rankin* [2009, 2012].

182 The parallel elongation of the distribution function at low energy is the result of two  
 183 factors; the parallel drift of a portion of the distribution function to carry the parallel  
 184 current and the plateauing of the distribution function associated with Landau damping  
 185 effects [e.g. *Watt and Rankin*, 2009]. The magnitude of the parallel drift will be propor-  
 186 tional to the magnitude of the parallel current while the plateauing will occur around the  
 187 phase speed of the wave. In the limit of  $\rho_i = 0$ , this velocity is on the order of the Alfvén  
 188 speed which at  $l_{||} = 5 R_E \sim 1 \times 10^6$  m/s.

189 The reduction of the parallel current with the inclusion of  $\rho_i$  effects explains the reduced  
 190 parallel elongation of the distribution function in Figure 4c relative to Figure 4b as the  
 191 reduced current requires less particle drift to carry it and the reduced wave amplitude  
 192 means that the width of the plateau associated with Landau damping effects is also  
 193 reduced. The increased phase speed of the wave, relative to the  $T_i = 0$  case, moves the  
 194 resonance region very slightly toward the tail of the distribution, although it is not visible  
 195 because this is completely lost in the core of the distribution function evident in Figure  
 196 4c. A more detailed analysis of  $\rho_i$  effects on the electron distribution function evolution  
 197 will be left to a subsequent publication where we will explore a range of wave parameters.

Another consequence of including  $\rho_i$  effects is evident in Figure 4d which displays the perpendicular profile evident at  $l_{\parallel} = 5 R_E$ . The wave perturbation has become significantly broader in the  $T_i = 1$  keV case (even though this case is plotted at an earlier time) due to the perpendicular dispersion of wave energy associated with ion gyroradius effects. This broadening means that more significant electron acceleration occurs along adjacent field lines compared with the original perturbation in order to carry the parallel current. Strictly speaking, the wave profile also broadens in the  $T_i = 0$  case because of electron pressure effects, but since  $T_i \gg T_e$ , the ion temperature effects dominate the characteristics of the wave dispersion in the latter case. For  $l_{\parallel} \geq 8 R_E$  (refer to Figure 2b), electron inertial effects dominate. However, the broadening associated with these effects is also too small to significantly modify the perpendicular profile established by  $\rho_i$  effects in the KAW regime.

Finally, Figure 5a displays the profile of parallel current at the ionospheric boundary as a function of time. Consistent with the previous Figures 3 and 4c, the ionospheric magnitude of the parallel current in the  $T_i = 1$  keV case is significantly reduced relative to the  $T_i = 0$  case. This reduced current is reflected in the diminished high energy tail, in the  $T_i = 1$  keV case, illustrated in Figure 5b. This result confirms that even though the peak of the electron energization is occurring at this altitude (where the imposed perpendicular perturbations naturally taper to  $\lambda_e$  scales), the  $\rho_i$  effects dominant in the plasma sheet limit the extent of the energization. Additionally, the maximum in the parallel current density occurs about 7 seconds earlier in the  $T_i = 1$  keV ( $t \approx 30$  s) case due to the increased phase speed of the wave relative to the  $T_i = 0$  case ( $t \approx 37$  s). Although the “ionospheric boundary” in the simulation is high relative to the Earth

(in order to reduce computational costs), the propagation times predicted would not be greatly changed if we further reduced the altitude of the ionosphere in the model because the transit time is primarily constrained by slower wave propagation in the plasma sheet. By the time the wave reaches close to the ionosphere, the phase speed  $\sim 10^8$  m/s and so propagation through the remaining  $R_E$  to the realistic ionospheric altitude only adds a fraction of a second to the propagation time. When the ion temperature was further increased to 5 keV, the peak in the ionospheric parallel current occurred significantly earlier still at  $t = 15$  seconds, although the amplitude is much smaller because  $k_{\perp}\rho_i$  is larger.

Figure 5a also illustrates a longer temporal width to the pulse ionospheric signature in the  $T_i = 1$  keV case relative to the  $T_i = 0$  case. This increase is simply due to the fact that (from equation 7) the dependence of the phase speed on  $k_{\perp}\rho_i$  (which increases as the ionospheric boundary is approached) leads to a greater velocity difference between the leading and trailing edges of the pulse relative to the  $T_i = 0$  case.

#### 4. Conclusions

In this work, we have studied the propagation of a kinetic Alfvén wave pulse from the magnetotail to the ionosphere using a new self consistent Gyrofluid-Kinetic Electron model (GKE) in a dipolar topology and have explored how ion gyroradius effects modify the propagation characteristics of the pulse and the associated electron energization. While magnetotail kinetic Alfvén wave propagation has been considered previously in the context of kinetic simulations, we believe that this is the first effort to do so in a 2D dipolar topology propagating a pulse all the way from the plasma sheet to the ionosphere. It is found that the inclusion of  $\rho_i$  effects results in a significantly faster propagation time

for the pulse from the plasmashet to the ionosphere. For a KAW perturbation with  $\lambda_{\perp eq} = 0.1 R_E$  (along an  $L = 10$  field line), and assuming  $T_e = 100$  eV and  $T_i = 1$  keV (resulting in a value of  $k_{\perp}\rho_i \sim 1$  in the plasma sheet), the parallel current maximizes at the ionosphere about 7 seconds earlier relative to the  $T_i = 0$  case. This time difference increases with larger  $k_{\perp}\rho_i$ . The inclusion of  $\rho_i$  effects also results in an increased dispersion of wave energy perpendicular to the ambient magnetic field relative to the  $\rho_i = 0$  case.

In addition to the increased phase speed and dispersion as  $k_{\perp}\rho_i$  increases, the resulting  $j_1$  (and hence electron energization) is reduced for a given magnitude of the perpendicular electric field (even though the primary electron acceleration is taking place in the region above ionospheric boundary where  $\lambda_e$  effects dominate). This reduction occurs because a hot ion will, on average, see a reduced average perpendicular electric field relative to a colder counterpart, resulting in a reduced  $\vec{E} \times \vec{B}$  drift and ion polarization current. This reduced polarization current requires a reduced parallel current for closure and a correspondingly reduced electron energization to carry the parallel current (which is qualitatively consistent with the results of *Chaston et al.* [2003]).

Finally, while some of the  $\rho_i$  effects on magnetospheric Alfvén waves discussed here can be derived from a gyrofluid description alone, such studies miss the all important self-consistent coupling to kinetic electrons which is crucial to improve our understanding of the electron energization and wave damping. Therefore, the model presented here is an important advancement to gyrofluid descriptions alone and we will use it to further explore the details of the wave-electron interactions for a range of realistic wave and plasma parameters in a follow-up investigation.



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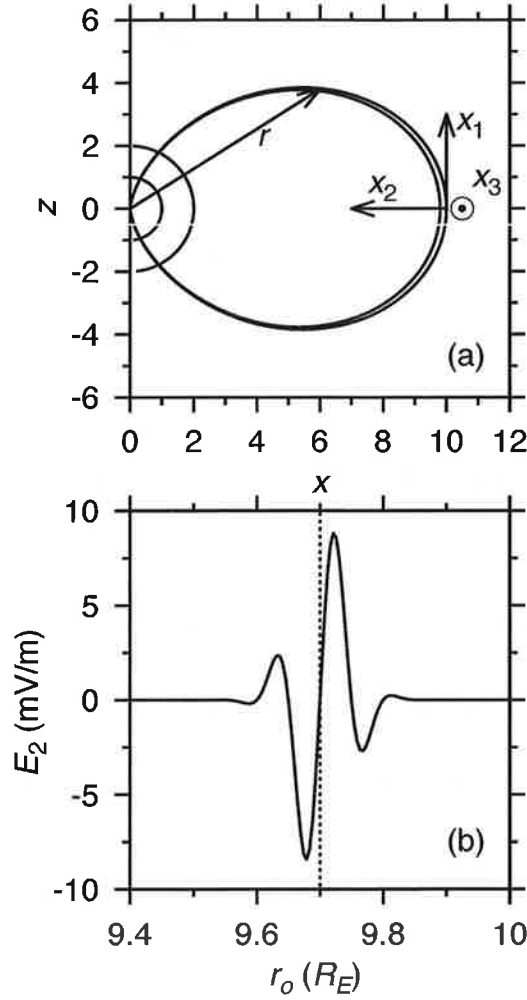
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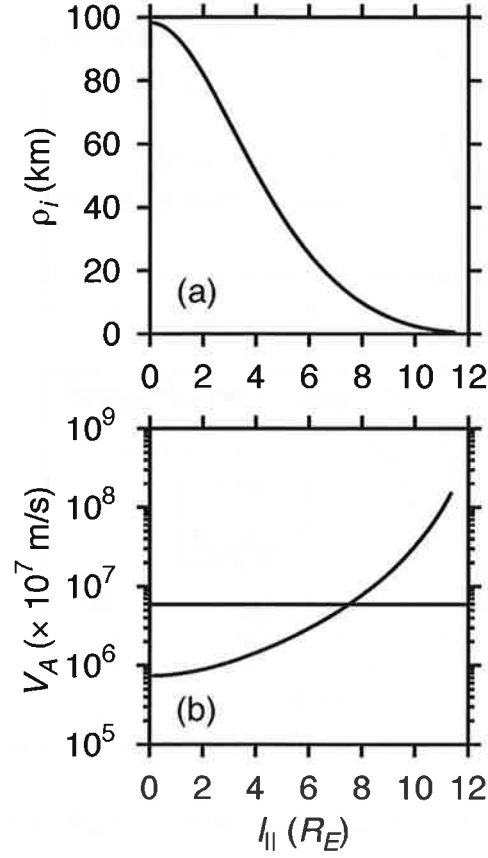
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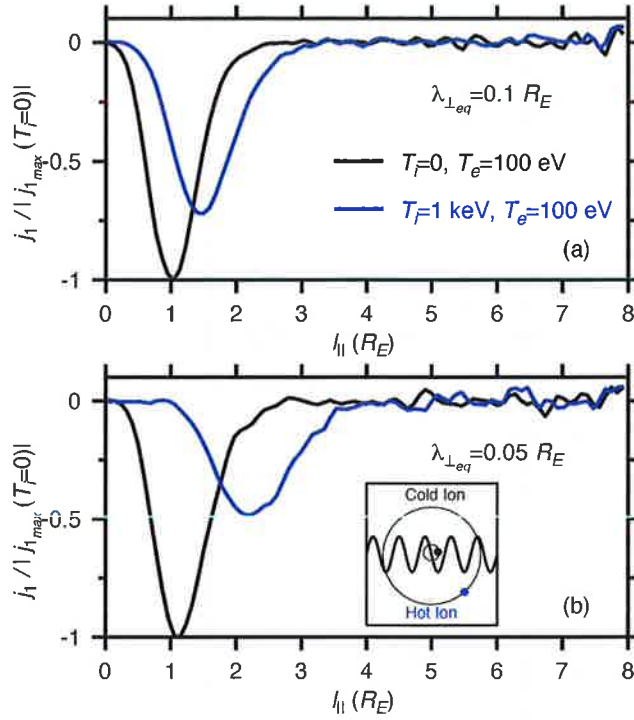
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**Figure 1.** a): Simulation domain where  $x_3$  is positive increasing out of the page. The circles of radius 1 and 2  $R_E$  respectively denote the surface of the Earth and “ionospheric” boundary. The angle  $\theta$  is subtended from the  $z$  axis. After *Damiano et al.* [2007]. b) Initial radial ( $E_2$ ) electric field profile as a function of  $r_o$  at the equator for  $L_\perp = 0.1 R_E$ .

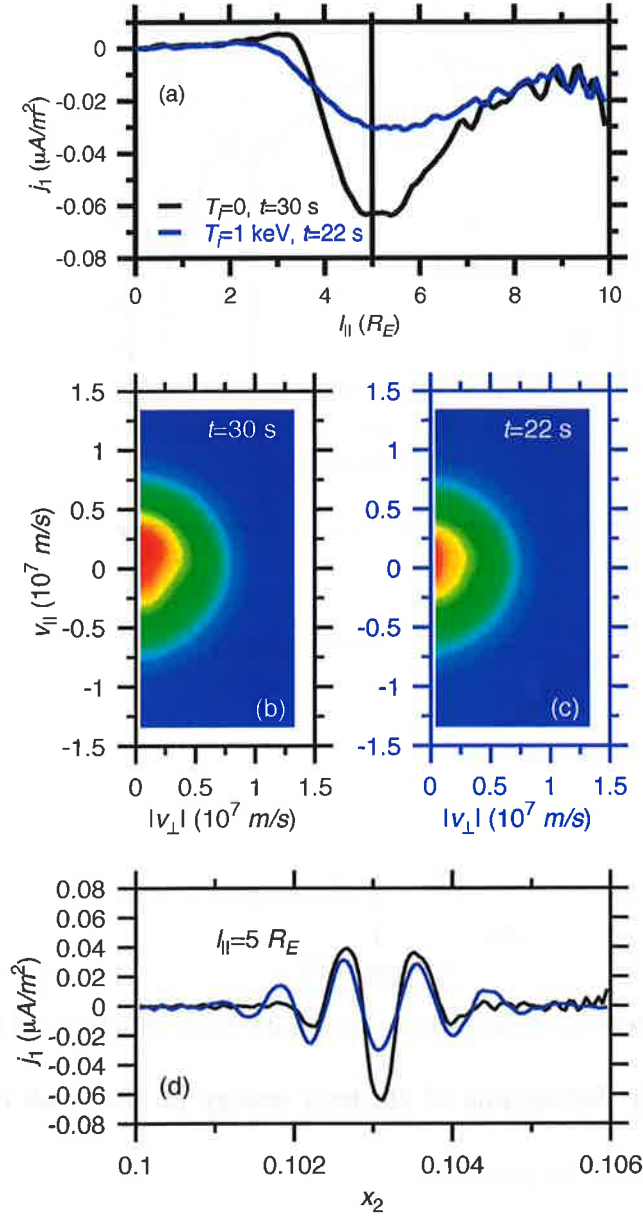


**Figure 2.** a) Ion gyroradius profile for  $T_i = 1$  keV as a function of length along the field line ( $l_{\parallel}$ ) measured from the equator in  $R_E$ . b) Alfvén velocity profile as a function of  $l_{\parallel}$ . The dotted horizontal line denotes  $v_{th} = V_A$ .

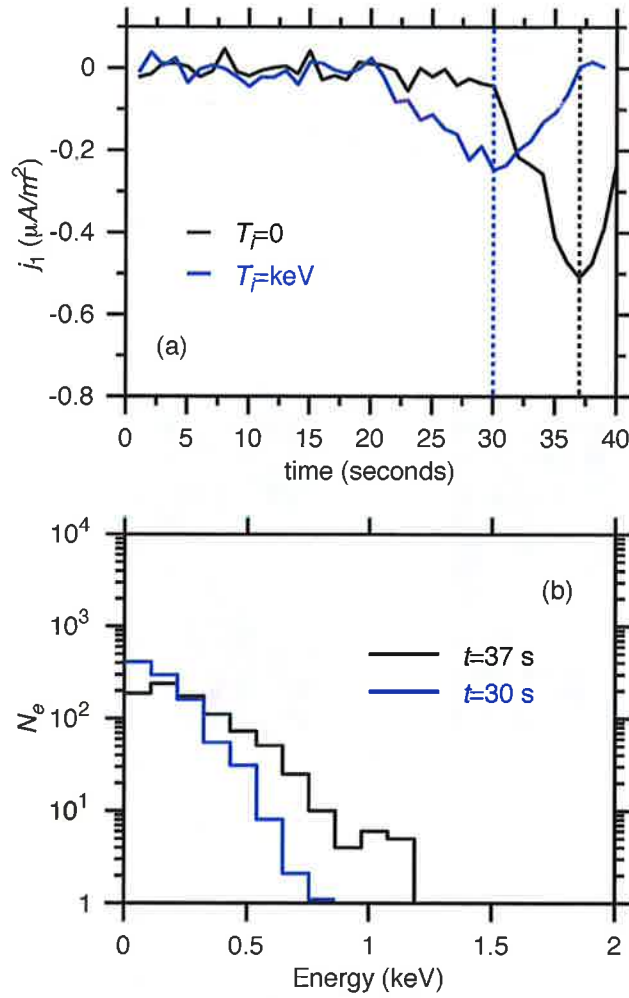


**Figure 3.** a) Parallel current density along  $r_o = 9.7$  field line at  $t = 8$  seconds, normalized by the absolute value of the maximum current amplitude in the  $T_i = 0$  case, as a function of  $l_{||}$ . b) Same, but for  $\lambda_{\perp eq} = 0.05 R_E$ . Inset: Cartoon of cold and hot ion orbits relative to the perpendicular electric field in a kinetic Alfvén wave. The hot ion feels a smaller orbit averaged perpendicular electric field ( $\langle E_{\perp} \rangle$ ) than a cold ion interacting with the same wave.





**Figure 4.** (a) Parallel current density along  $r_o = 9.7$  as a function of length along the field line (measured from the equator) for the  $T_i = 0$  (black) and  $T_i = 1$  keV cases (blue) at indicated times. (b) Distribution function at  $l_{||} = 5 R_E$  (indicated by vertical black line in panel (a)) for case of  $T_i = 0$  and  $t = 30$  seconds. (c) Same, but for case with  $T_i = 1$  keV and  $t = 22$  seconds. (d) Perpendicular profile of parallel current density at  $l_{||} = 5 R_E$  at times indicated in panel (a).



**Figure 5.** a) Parallel current at ionospheric boundary as a function of time for same parameters as Figure 4a. b) Histograms of electron energy at the peak of the parallel current in each case as indicated in panel (a).

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