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# **1 External vs Internal Triggering of Substorms: An 2 Infomation-Theoretical Approach**

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3 The role of external triggering of substorms through northward turning  
4 of the interplanetary magnetic field has been examined in a number of re-  
5 cent studies [*Hsu and McPherron*, 2002; *Morley and Freeman*, 2007]. While  
6 *Hsu and McPherron* [2002, 2004] argue that the strong association between  
7 external triggers defined by *Lyons et al.* [1997] and substorm onsets could  
8 be responsible for most substorms, *Morley and Freeman* [2007] argue that  
9 the association between northward turnings and substorm onsets are con-  
10 incidental rather than causal, because the same external triggers are also closely  
11 associated with an artificial list of substorm onsets generated with the Min-  
12 imal Substorm Model [*Freeman and Morley*, 2004], which has no requirement  
13 of northward turning. We examine an expanded list of substorms [*Frey et al.*,  
14 2004; *Frey and Mende*, 2006] using conditional redundancy, an entropy-based  
15 measure of conditional dependency, to examine whether northward IMF turn-  
16 ing as an external trigger provides any additional information about substorm  
17 onset beyond knowing that there has been a period of sustained loading of  
18 energy flux (southward IMF). Our analysis reveals that only a few percent  
19 additional information is provided by the northward turning criterion, which  
20 is consistent with the statistics of surrogate datasets of external triggers con-  
21 structed to coincide with 2% of substorms. We therefore conclude that north-  
22 ward turning of the IMF is, in general, coincidentally, rather than causally,  
23 associated with substorm onsets.

## 1. Introduction

24 The solar wind transfers energy into the magnetosphere, and correlation studies have  
 25 established that energy flux is particularly strong when the interplanetary magnetic field  
 26 (IMF) is southward. The magnetosphere responds to this energy flux in a complex manner,  
 27 leading to large-scale activity such as strong convection or substorms. Understanding  
 28 the underlying cause of substorm onset remains a central problem in space physics. One  
 29 significant question is whether substorms are triggered externally (for example by changes  
 30 in the IMF) or whether they are primarily an internal response that results when stored  
 31 energy in the magnetotail exceeds a critical threshold.

32 Lyons [1995] proposed that the expansion phase of substorms results from a reduction in  
 33 the large-scale convection electric field imparted to the magnetosphere from the solar wind  
 34 following a period of strong magnetospheric convection (growth phase). This proposal was  
 35 supported by observations suggesting that northward IMF turnings following a period of  
 36 IMF  $B_z$  that has been negative for more than 30 minutes triggers substorm onset [*Caan*  
 37 *et al.*, 1975; *Rostoker*, 1983; *McPherron et al.*, 1986]. A subsequent observational study  
 38 that employed coordinated observations to identify substorm onsets and compare with  
 39 external triggers suggested a high likelihood to see an external trigger in conjunction with  
 40 a substorm onset, where a trigger satisfies the following requirements [*Lyons et al.*, 1997]:

- 41 1. Growth Phase Requirement:  $B_z < 0$  for 22 of the previous 30 minutes
- 42 2. Turning Initiation:  $B_z(t_0 + \Delta t) - B_z(t_0) \geq 0.375\text{nT}\Delta t/\text{min}$
- 43 3. Sustained:
  - 44 •  $\nabla B_z(t : t + 10) \geq 1.75\text{nT}/\text{min}$

$$\bullet B_z(0 \leq t - t_0 \leq 3\text{min}) \geq B_z(t) + 9.15 * (t - t_0)\text{nT}/\text{min}$$

$$\bullet B_z(3\text{min} \leq t - t_0 \leq 10\text{min}) \geq B_z(t) + 0.45\text{nT}$$

4. No other point in the previous 10 minutes is a trigger

A more quantitative investigation was subsequently performed by *Hsu and McPherron* [2002, 2003, 2004] using a substorm onset database determined from a decrease in the AL index in association with Pi2 pulsations. In that work they examined the association number between substorm onsets and triggers (which is like a cross-correlation) and found that there is a strong association between substorm triggers as defined above and substorm onsets. In their subsequent work, *Hsu and McPherron* [2004] examined the relative number of events and found that while most of the substorms could be associated with a trigger that nearly 40% were not associated with a trigger, which they considered to be evidence that substorms are caused by an internal instability. However, they suggested that the internal instability is susceptible to external perturbations as evidenced by the strong association of the substorms with external triggers.

Internal triggering of substorms is believed to result when sustained energy flux is stored up in the magnetotail leading to stretching of the tail and intensification of cross-tail current. When the energy stored in the tail attains a critical threshold energy is released as the result of a physical processes such as an internal instability [*Lui*, 1996; *Cheng and Lui*, 1998] or reconnection [*Birn and Hones*, 1981; *McPherron*, 1991]. The underlying dynamics of storage and release have been captured by simpler models such as a dripping faucet model *Baker et al.* [1990] or integrate and fire model such as the Minimal Substorm Model (MSM) [*Freeman and Morley*, 2004] or through circuit analogues [*Horton*

67 *and Doxas, 1996*]. The basic underlying feature of storage and release models is that there  
68 is an energy input  $dE/dt = P(\text{solarwind})$  that results when IMF is southward and the  
69 energy level is reset to a “ground state” dependent on the external boundary conditions  
70 (bc) ( $E \rightarrow E_0(\text{bc})$ ) when the energy level exceeds a critical level  $E > E_c$ .

71 *Morley and Freeman [2007]* reevaluated the data set considered by [*Hsu and McPher-*  
72 *ron, 2002*] considering the importance of internal vs external triggering. While their  
73 analysis confirmed that there is a high association number between external triggers and  
74 substorm onsets, they also considered whether the association was causal or coincidental.  
75 To gain some insight, they defined an internal trigger as a period when the IMF has been  
76 southward at least 22 of the previous 30 minutes (equivalent to criterion 1 of the exter-  
77 nal trigger). Using only these “internal” triggers they found that there is also a strong  
78 association between “internal” triggers and substorm onsets. As a test of the relevance of  
79 northward turning for substorm onset, they considered a stream of solar wind data and  
80 constructed an alternative data set of substorm onsets using the integrate and fire MSM  
81 model. This alternative set of substorm onsets only depends on the energy input from the  
82 solar wind and has no dependence on northward turning of the IMF. However, when they  
83 performed a comparison of the external triggers with the alternative substorm data set,  
84 they found a strong association number in spite of the fact that these substorm onsets had  
85 no requirement of northward turning. The conclusion that they drew was that although  
86 northward turnings are correlated with substorms, they are not causally correlated with  
87 substorms. Following up on this study, [*Freeman and Morley, 2009*] used a superposed  
88 epoch analysis of IMF  $B_z$  with respect to substorm onset time to show that the tendency

89 of the IMF to turn northward close to substorm onset could be explained simply by a bias  
 90 of substorms to occur during southward IMF irrespective of a coincident rapid northward  
 91 turning of the IMF, and similar results were found for MSM substorms, which have no  
 92 northward turning requirement. [Newell and Liou, 2011] similarly noted that although  
 93 the mean  $B_z$  has a northward turning (reversion to the mean) starting 20 minutes before  
 94 onset, a similar reversion to the mean was found for random elevations of solar wind driv-  
 95 ing based on several coupling functions, further supporting the concerns of *Morley and*  
 96 *Freeman* [2007]. These analyses cast doubt on the hypothesis that northward turning of  
 97 the IMF is causally related to substorm onset by providing simple alternative explanations  
 98 for the association of the external trigger and the onset. However, these analysis do not  
 99 directly address the question of whether northward IMF is causally related to substorm  
 100 onset.

101 To address this issue we utilize information theory to analyze the following question:  
 102 do external triggers (that satisfy 1-4 above) provide any additional information about  
 103 substorm onsets beyond what is known from the energy flux into the system (criterion 1),  
 104 and if so, how much more information is known. To answer this question we will utilize  
 105 redundancy, which is an entropy-based measure of dependency.

## 2. Redundancy as a measure of dependency

*Fraser* [1989] and *Prichard and Theiler* [1995] pioneered the use of redundancy as a generalization of mutual information to examine multi-dimensional systems. To examine dependency between a set of variables that are measured, it is useful to consider whether

$$P(x_1, x_2, \dots, x_n) \stackrel{?}{=} P(x_1)P(x_2)\dots P(x_n). \quad (1)$$

with  $P(x_1, x_2, \dots, x_n)$  the joint probability of measuring a combination of variables and  $P(x_1), \dots, P(x_n)$  the probability of measuring each of the variables separately. This relationship is preferable to examining cross-correlations because it allows more generally for nonlinear dependencies, which, in the case of substorms, should be considered given that substorm response is highly nonlinear. The question posed in Eq. 1 can be quantified using the following definition of redundancy as a discriminating statistic [Prichard and Theiler, 1995]

$$R(x_1; \dots; x_m) = \sum_i H_1(x_i) - H(x_1; \dots; x_m) \quad (2)$$

106 which measures how much additional information is known about the relationship of set of  
107 variables  $(x_1; \dots; x_m)$  when they are measured simultaneously rather than independently.

In the expression for redundancy,  $H_1(x_i)$  is the entropy of measuring variable  $x_i$  defined as

$$H_1(x_i) = - \sum_{\aleph} p(\hat{x}_i) \log p(\hat{x}_i) \quad (3)$$

where  $p(\hat{x}_i)$  is the probability that the variable,  $x_i$ , lies in the partition,  $\hat{x}_i$ , of a set of discrete partitions of the domain,  $\aleph$ . Similarly, the joint entropy is obtained using

$$H(\mathbf{x}) = - \sum_{\aleph} p(\hat{\mathbf{x}}) \log p(\hat{\mathbf{x}}) \quad (4)$$

108 with  $\mathbf{x} = (x_1, \dots, x_n)$  and  $\hat{\mathbf{x}} \in \aleph$ .

In the case that none of the variables are related to each other, there is no redundancy and  $R = 0$ . Here, we are more interested in looking at conditional dependencies that are better described by marginal redundancy, which provides a measure of how much a

variable,  $x_m$  depends on a set of other variables,  $(x_1, \dots, x_{m-1})$

$$R_M(x_1, \dots, x_{m-1}; x_m) = R(x_1; \dots; x_m) - R(x_1; \dots; x_{m-1}). \quad (5)$$

In this study, we are particularly interested to know how an output,  $x_m$ , depends on another variable,  $x_1$ , given a vector of other inputs,  $(x_2, \dots, x_{m-1})$ . The conditional redundancy

$$R_C(x_1|x_2, \dots, x_{m-1}; x_m) = R_M(x_1, \dots, x_{m-1}; x_m) - R_M(x_2, \dots, x_{m-1}; x_m) \quad (6)$$

109 provides such a measure and allows us to determine if a given variable provides additional  
 110 information beyond what we know from another set of inputs or whether that variable  
 111 contains redundant information.

We can now state the question raised by the analysis of *Morley and Freeman* [2007] as a conditional redundancy. Is there any additional information about substorm onsets provided by external triggers (defined by conditions 1-4) given that the condition for “internal” triggering (condition 1) is known. This information is quantified by  $R_C(\text{ext}|\text{int}; \text{onsets})$  and can be compared with  $R_M(\text{ext}, \text{int}; \text{onsets})$  to obtain the fraction,  $\mathcal{F}$ , of additional information provided by knowledge of external triggers

$$\mathcal{F} \equiv \frac{R_C(\text{ext}|\text{int}; \text{onsets})}{R_M(\text{ext}, \text{int}; \text{onsets})} \quad (7)$$

112 In the case that onsets are mostly determined by external triggering independent of the  
 113 loading rate  $\mathcal{F} \rightarrow 1$ , while in the case that there is no dependence on external triggers,  
 114  $\mathcal{F} \rightarrow 0$ .

### 3. Database for substorm analysis

115 For our analysis, we consider the substorm onset list obtained by *Frey et al.* [2004] and  
116 *Frey and Mende* [2006]. These onsets were obtained using the FUV instrument on the  
117 IMAGE spacecraft. Substorms were identified if they fulfilled the following criteria: (1)  
118 a clear local brightening of the aurora has to occur, (2) the aurora has to expand to the  
119 poleward boundary of the auroral oval and spread azimuthally in local time for at least  
120 20 min, (3) a substorm onset was only accepted as a separate event if at least 30 min  
121 had passed after the previous onset. The dataset contains over 2400 substorms during  
122 2000-2005.

123 We also examined triggers in solar wind data defined by criteria (1-4) above using  
124 satellite measurements. Our primary source of data was the ACE satellite. We augmented  
125 the ACE data with WIND observations when ACE data was not available. Data gaps  
126 less than 5 minutes in duration were filled in using linear interpolation as in the study  
127 of *Morley and Freeman* [2007]. The data was propagated using the minimum variance  
128 method to  $GSM(x,y,z) = (17,0,0) R_E$  [*Weimer et al.*, 2003].

129 For our analysis, we construct three variables (int,ext,onset) which take on the value of  
130 0, 1, or NaN. Variable int=1 if criterion (1) is satisfied at the time of observation, int=0  
131 if criterion (1) is not satisfied, and int=NaN if inadequate data is available to address  
132 criterion (1). Similarly, ext=0,1,NaN when criteria (1-4) are not all satisfied, all satisfied,  
133 or not enough data is available to assess criteria (1-4). In evaluating criteria (1-4)  $\Delta t$  is  
134 taken to be 1 minute. The variable onset=1 when there is a substorm onset and onset=0  
135 otherwise. The data streams are obtained for every minute of data during the period

136 between the first and last substorm of the *Frey et al.* [2004]; *Frey and Mende* [2006] data  
137 list.

138 It is useful to first examine the statistics of substorm onsets and external triggers. In  
139 Figure 3 we show (a) the intersubstorm intervals obtained by considering the difference in  
140 onset times of the ordered list of substorms. Consistent with the data selection criterion  
141 of *Frey et al.* [2004] there are no intersubstorm intervals less than 30 minutes. A peak does  
142 appear at around 1 hour and a second peak at around 3 hours. The three hour peak has  
143 been previously reported [*Borovsky et al.*, 1993; *Prichard et al.*, 1996] and was interpreted  
144 as a periodic component that occurs in spite of random solar wind driving. They suggested  
145 that the three-hour timescale is an intrinsic property of the magnetosphere related to  
146 internal dynamics. It is also interesting to note a broad peak on the intersubstorm interval  
147 between 10-15 hours and at 25 to 30 hours. These peaks are likely an orbital bias that  
148 result from the 14.2 hour orbital period of the IMAGE spacecraft. Such a periodicity  
149 would arise because the imager was turned off during passage through the radiation belt  
150 and targeted the auroral oval, which would repeat on a timescale of 14 hours. For our  
151 analysis, this orbital bias is not relevant, because we consider timescales that are less than  
152 five hours as shown in panel (b).

153 Northward turning intervals were also identified in the data, and we have examined the  
154 statistics of northward turning intervals, which we have shown in panel (c) with the same  
155 time resolution as panel (b). It is to be noted that the smallest interval is 10 minutes  
156 consistent with criterion (4) for an external trigger. The distribution of northward turning  
157 intervals appears to fall off exponentially like those of a Poisson process suggestive that

158 northward turning is a somewhat random process. A comparison of panels (b) and (c)  
 159 shows that the statistics of intersubstorm onset intervals is quite different than northward  
 160 turning intervals.

#### 4. Analysis of substorm redundancy

161 In this section, we compute the conditional redundancy using the int, ext, and onset  
 162 datastreams. It is necessary to compute

$$R_C(\text{ext}|\text{int}; \text{onset}) = R_M(\text{int}, \text{ext}; \text{onset}) - R_M(\text{int}; \text{onset}) \quad (8)$$

$$= R(\text{int}, \text{ext}, \text{onset}) - R(\text{int}, \text{ext}) - R(\text{int}, \text{onset}) + R(\text{int}) \quad (9)$$

$$= H(\text{ext}, \text{int}) + H(\text{int}, \text{onset}) - H(\text{ext}, \text{int}, \text{onset}) - H(\text{int}) \quad (10)$$

163 The entropies are computed from the joint probabilities functions:  $p(\text{ext}, \text{int}, \text{onset})$ ,  
 164  $p(\text{int}, \text{onset})$ ,  $p(\text{ext}, \text{int})$ ,  $p(\text{int})$  via Eq. 4. It is useful to consider a few limiting cases. If on-  
 165 sets could be entirely determined from criterion (1), then  $p(\text{int}, \text{onset}) = p(\text{onset}) = p(\text{int})$   
 166 in which case  $R_C(\text{ext}|\text{int}; \text{onset}) \rightarrow 0$ . In the case where onsets have no dependence on cri-  
 167 terion (1), then  $R_C(\text{ext}|\text{int}; \text{onset}) \rightarrow H(\text{ext}) + H(\text{onset}) - H(\text{ext}, \text{onset}) \equiv M(\text{ext}, \text{onset})$ ,  
 168 where  $M$  is the mutual information [Prichard and Theiler, 1995].

169 Because data only appears in binary, the distributions for  $p(x_1, x_2, x_3)$  are simply com-  
 170 puted by converting data to binary numbers ( $x_1 = 1, x_2 = 0, x_3 = 1 \rightarrow 101 = 5$ ). A  
 171 number is obtained for each measurement, then the numbers are sorted and instances are  
 172 counted. Division of the total instances of each number by the total number of observa-  
 173 tions provides the probability for that number. Entropy involves summing  $p \log p$  for each  
 174 number.

175 Because the entropy is based on probabilities, the statistics will depend on the time  
 176 resolution. To explore this effect, we constructed resampled variables,  $\bar{a}$ , that consider  
 177 whether a trigger or onset occurs within a window of  $\pm h$  minutes around time,  $t$ . More  
 178 specifically,  $\bar{a}(t) = 1$  if any of  $\{a(t-h), \dots, a(t+h)\} = 1$ ,  $\bar{a}(t) = \text{NaN}$  if all of  $\{a(t-h), \dots, a(t+h)\} = \text{NaN}$ , and  $\bar{a}(t) = 0$  otherwise. A similar windowing was used in prior  
 180 studies of association number to improve statistics [*Hsu and McPherron, 2002; Morley and Freeman, 2007*]. In the present study, it should be noted that both the triggers and  
 182 onsets are both windowed, so the overlap between a trigger and onset occurs when they  
 183 are separated by  $2h$ . In the following analysis, we present results with  $h = 5$ , which  
 184 provides good statistics without overly smoothing the results.

185 The results of our analysis are shown in Figure 2. Panel (a) shows in blue the conditional  
 186 redundancy of the dependence of substorm onsets (at a given time lag,  $\tau$ ) on external  
 187 triggers given the internal trigger [i.e.  $R_C(\text{ext}(t)|\text{int}(t); \text{onset}(t+\tau))$ ] and for comparison  
 188 the conditional redundancy when the list of external triggers is randomized in red. It  
 189 is apparent that  $R_C$  is elevated with respect to random triggers around substorm onset  
 190 and there are secondary elevations at 50 minutes and a 3 hours after the external trigger.  
 191 The secondary elevations correspond with peaks seen in the statistics of intersubstorm  
 192 intervals shown in Figure 3. To place these elevations into context, in panel (b) we show  
 193  $R_C(\text{int}(t)|\text{ext}(t); \text{onset}(t+\tau))$ , which indicates how much additional information about  
 194 substorm onset is provided from the growth phase requirement beyond that which is  
 195 known from the northward turning requirement. The peak is a factor of 25 larger than  
 196 that seen in panel (a) suggestive that external triggers only provide an additional 4% more

197 information. The internal trigger peak occurs at 15 minutes following onset with a broad  
198 distribution with a full width at half maximum around 1 hour. Secondary elevations seen  
199 in panel (b) occur at 2 hours and 3 hours and do not coincide with the peaks seen in panel  
200 (a).

201 To further interpret the value of the conditional redundancy obtained in our analysis,  
202 we also perform a comparison with a surrogate dataset of external triggers constructed  
203 using the onset list. Holding the number of external triggers fixed, we select a percentage  
204 of the onsets to coincide with the onsets, and the remainder of the external triggers are  
205 randomized. Panel (c) shows the conditional redundancy when 20 percent of the external  
206 triggers are selected to coincide with onsets and the remainder of the external triggers are  
207 randomized. As expected, the peak coincides with substorm onset and is dramatically  
208 elevated (factor of 50) compared with that due to northward turning.

209 Panel (d) shows the significance of external triggering and the fractional information  
210  $\mathcal{F}$  is indicated by the color. The significance is obtained from  $S = |R_C - \mu|/\sigma$  where  $\mu$   
211 and  $\sigma$  are the mean and spread of the surrogate dataset of randomized triggers shown in  
212 panel (a). There is clearly a peak of significance suggestive that some substorms may be  
213 triggered; however, because the fractional information for the peak is small,  $\mathcal{F} \approx 0.04$ , it  
214 is likely that only a few substorms are triggered. The increase of  $\mathcal{F}$  away from the onset  
215 peak results from a reduction of information from substorm growth phase

216 To further quantify how many substorms are triggered, we construct surrogate datasets  
217 as in panel (c) where the fraction of substorms that are triggered varies from 0 to 100%.

218 The results presented in Figure 3 show that the value of conditional redundancy obtained  
219 in panel (a) is consistent a dataset constructed with 2% triggered substorms.

## 5. Conclusions

220 Prior work has suggested that northward turning of the IMF is closely associated with  
221 substorm onset. Questions have arisen about whether this association is coincidental or  
222 causal. In this paper, we have provided a quantitative analysis, based on conditional  
223 redundancy, that demonstrates that northward turning of the IMF is, in general, coin-  
224 cidental with substorm onsets rather than causal. This finding is consistent with the  
225 analysis of *Freeman and Morley* [2009] and *Newell and Liou* [2011], which suggested that  
226 the association between northward turning of the IMF is most likely an indicator of a  
227 reversion to the mean rather than a trigger. Increased driving of the magnetosphere  
228 through other coupling functions also showed a similar northward turning of the IMF  
229 consistent with a reversion to the mean. These results are consistent with the study of  
230 *Morley and Freeman* [2007], which suggested that artificial substorms, essentially driven  
231 only by a coupling function, are well associated with northward IMF turnings. *Newell*  
232 *and Liou* [2011] also points out that southward IMF turnings would be equally likely to  
233 be associated with substorm onset.

234 This example also demonstrates the feasibility of using information-theoretical tools,  
235 such as conditional redundancy, to determine whether correlations are coincidental or  
236 causal in nature. Because these tools are founded on statistics, they should be applied  
237 to datasets of sufficient size to ensure convergence of the multivariate probabilities, and  
238 the results should be compared with surrogate data sets to establish its significance.

239 These techniques could be used to address causal roles of solar interplanetary structures  
240 on the wave environment of the inner magnetosphere and radiation belt responses or to  
241 understand identify the causal roles of waves, field aligned currents, electron precipitation,  
242 and ion outflows in the coupled magnetosphere-ionsosphere system [e.g. *Strangeway et al.*,  
243 2005].

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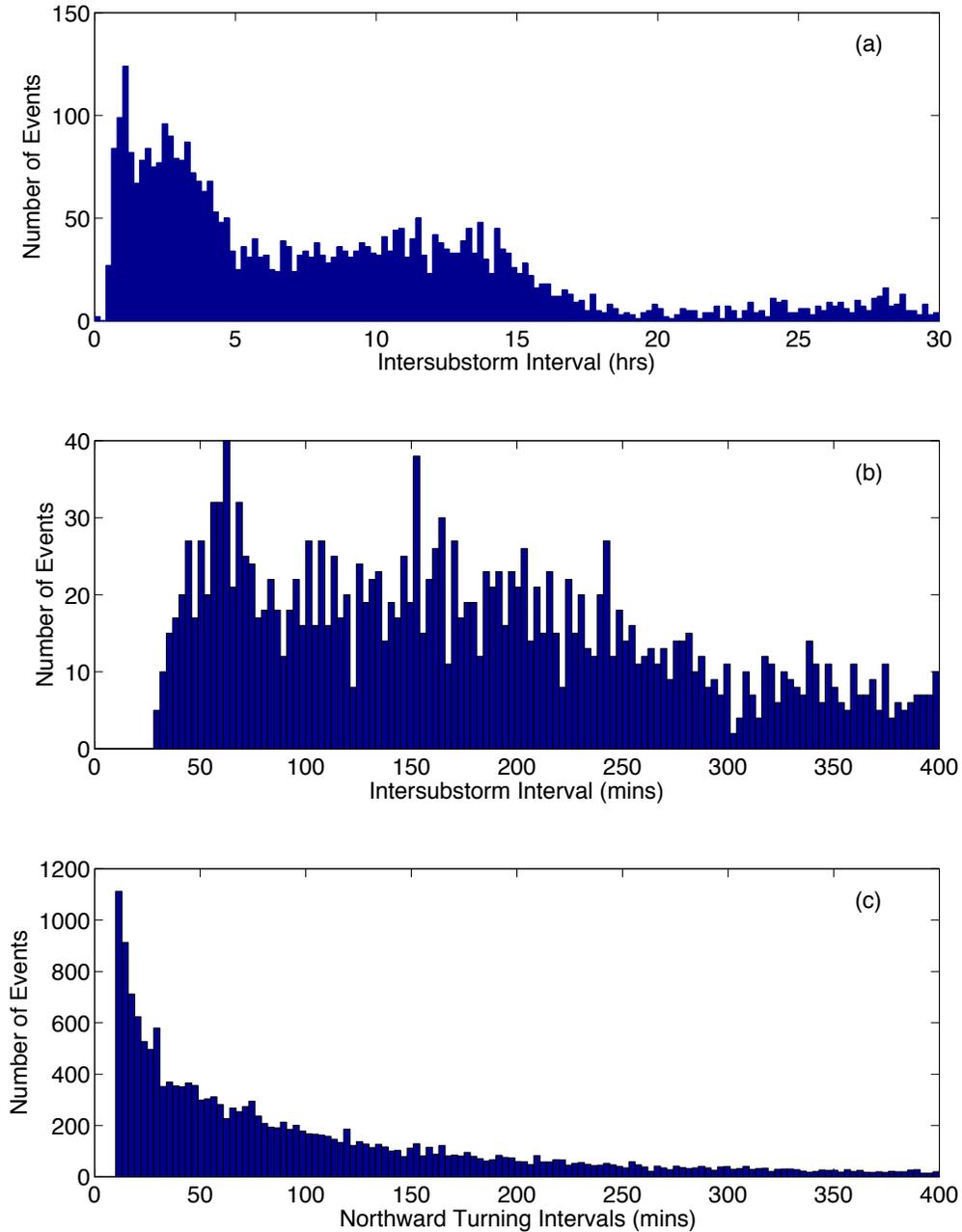
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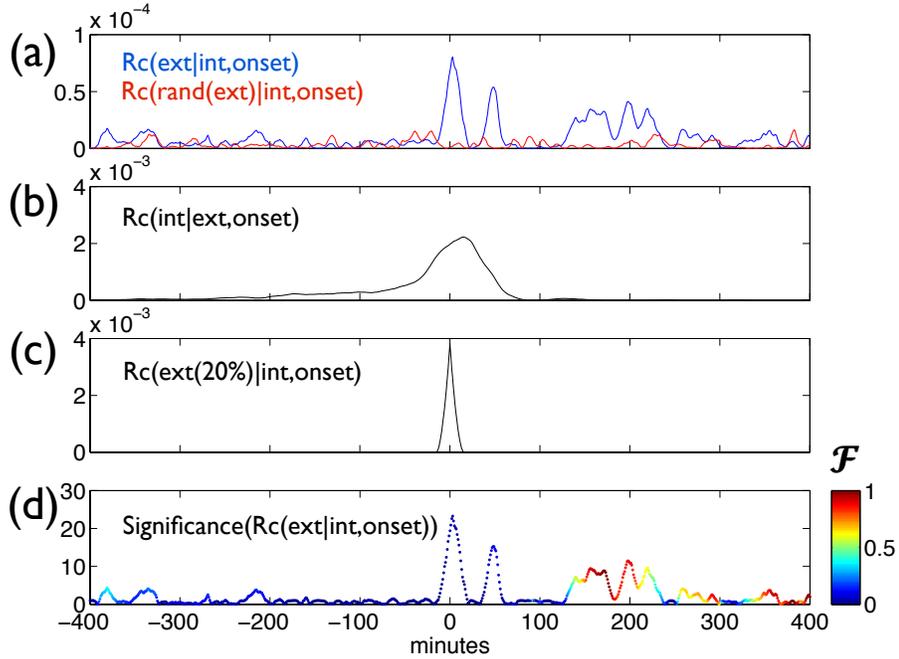
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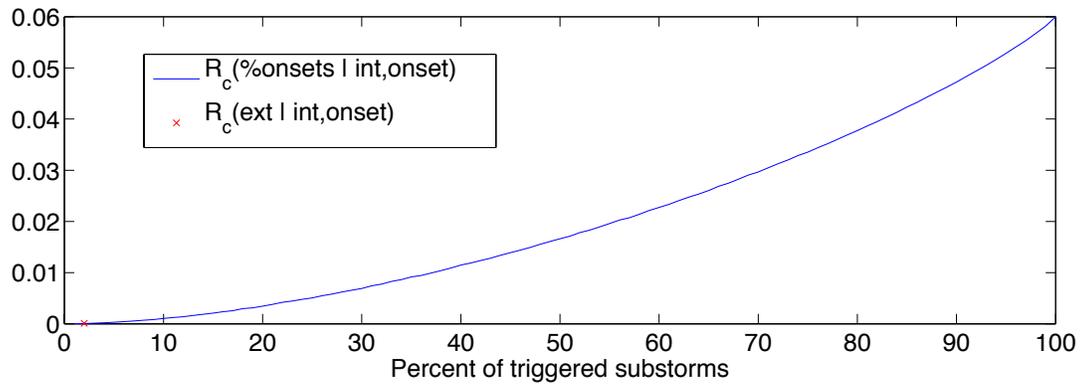
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**Figure 1.** Statistics of substorms and external triggers. Panels (a) and (b) show the statistics of intersubstorm intervals (on hour and minute timescales). Panel (c) shows the statistics of external triggers defined as sustained northward IMF turning following a growth phase.



**Figure 2.** Conditional redundancy describing how much additional information about onsets,  $R_C(\text{ext}(t)|\text{int}(t); \text{onset}(t + \tau))$ , is added by knowing external trigger events (ext) given the growth phase requirement (int), as a function of  $\tau$  for: (a) external triggers satisfying *Lyons* [1995] (blue) and random external triggers (red), (b)  $R_C(\text{int}(t)|\text{ext}(t); \text{onset}(t + \tau))$ , (c) 20 percent of external triggers coincide with onset list and the remainder are random, and (d) the significance of the external trigger compared with random triggers with the fractional information,  $\mathcal{F}$ , shown in color.



**Figure 3.** The conditional redundancy of datasets constructed with a percentage of onsets externally triggered and the remainder of the external triggers randomized is compared with the peak of conditional redundancy from Figure 2, which is consistent with a dataset of external triggers constructed with 2% accuracy.

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