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Response to "Comment on 'Turbulent equipartition theory of toroidal momentum pinch' " [Phys. Plasmas, 15, 055902 (2008)]

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(Dated: February 13, 2009)

Abstract

This response demonstrates that the comment by Peeters *et al.* contains an incorrect and misleading interpretation of our paper [Hahm *et al.*, Phys. Plasmas **15**, 055902 (2008)] regarding the density gradient dependence of momentum pinch and the turbulent equipartition (TEP) theory.

The subject discussed in this reply is in relation to the recent theoretical predictions of a parallel momentum pinch in toroidal geometry. The main purpose of our recent paper¹ was to elucidate the physics associated with that pinch in the context of the TEP (turbulent equipartition) theory which relies on local conservation properties, and mixing of a magnetically weighted quantity. Following upon a rather lengthy derivation² based on the gyrokinetic equation which includes both the TEP pinch which is mode-independent, and the curvature driven thermoelectric pinch which is mode-dependent, we reported a more concise physicsoriented interpretation of the TEP pinch.^{1,3} We've formulated the problem in terms of the angular momentum density based on a conservative gyrokinetic equation in general toroidal geometry.⁴ On the other hand, Peeters et al.,⁵ have formulated the pinch in terms of the Coriolis force which appears in the rotating frame. The actual analytic derivation has been performed in a shearless slab geometry, but with the Coriolis and magnetic drifts kept with the purpose to derive a momentum pinch for a pure ion temperature gradient (ITG) mode with an adiabatic electron response. They dealt with the parallel flow (without a density multiplier). With these differences in approaches, emphases, and also in ensuing approximations, there have been some misunderstandings and improper interpretations of our work and their own work in their comment.⁶

The comment by Peeters $et \ al.,^6$ contains the following claims with which we disagree based on technical grounds:

i) The linear dependence on density gradient length, in the pinch to diffusivity ratio expression in their letter,⁵ comes from the Coriolis drift.

ii) Their result for the ITG mode with an adiabatic electron response contains our TEP formulation.

Their comment⁶ also includes a figure comparing the pinch to diffusivity ratio from a numerical calculation, from a reformulation of their formula, and from our original expression. Since those were obtained under different assumptions and for different physical models, in particular, inclusion of trapped electrons, and parameters, we find their comparison to be misleading. We clarify these issues in this reply.

I. MAIN DIFFERENCE BETWEEN OUR PAPERS AND THEIR LETTER

The main focus of our paper on the TEP momentum pinch¹ was on physics understanding which is independent of the particle flux model and also of the specific modes such as the ITG or trapped electron mode (TEM). Our preceeding paper illustrated details of derivations from the gyrokinetic equation.² Throughout the derivation, manifestations of new terms, which came from the original conservative gyrokinetic equations,⁴ have been carefully studied and discussed. It's crucial to remember that we have identified the "curvature driven thermoelectric (CTh) pinch" in addition to the TEP pinch. This CTh pinch is proportional to the correlation between the ion temperature fluctuation (δT_i) and the potential fluctuation ($\delta \phi$) weighted by the magnetic curvature and grad-*B* drift, ω_{di} (see Eq. (11), Eq.(39) and Eq.(66) of Ref. 2). We've not claimed that our TEP pinch is the full story (see conclusions in Refs. 1,2), but emphasized that the TEP pinch depends only on the fluctuation amplitude and the decorrelation time, and is a mode-independent generic and robust feature (i.e., whether it's ITG or TEM).

On the other hand, in the derivation of Peeters *et al.*,⁵ intended for the pure ITG mode, the ion temperature evolution equation (Eq. (15) in Ref. 5) has *never* been used. Their derivation did not properly take into account a dynamical role of the ion temperature fluctuations, and therefore, could not describe physics associated with the CTh pinch in a realistic system.

Our theory is also formulated in general toroidal geometry, which allows shaping, with geodesic curvature, magnetic shear, etc., and did not make an assumption on the temperature ratio T_i/T_e . The effect of mode structure on the final answer has also been characterized by a dimensionless parameter $F_{balloon}$, which was calculated for parameters from actual experiments.² This is unlike the letter by Peeters *et al.*,⁵ where a local analysis has been performed with a fictitious Coriolis drift and magnetic drift in a system which is Galilean invariant in the direction of flow. They've also assumed equal temperatures, $T_i = T_e$. If one relaxes this condition, for a more direct comparison with our prediction, the derivation according to Peeters *et al.*⁵ would have led to a formula $V_{pinch}/\chi_{\phi} = -1/L_n - 4T_i/T_eR$, which is different from our TEP prediction,^{1,2} which is independent of T_i/T_e . For these reasons, it must be obvious that the TEP pinch *cannot* simply be a subset of their solution, as Peeters *et al.* claim based on the fact that they kept more terms. To set the record straight,

we'd like to mention that neither the phrase "TEP" nor the phrase "symmetry breaking mechanism" was ever used in their letter⁵. While they state that their simple analytic fluid model is for highlighting the physics effect, it's noteworthy that the Coriolis drift and the ballooning mode structure are incompatible with a system with Galilean invariance along a straight magnetic field. Table I summarizes the main difference between our papers and their letter. Finally, Peeters *et al.*'s comment⁶ contains an incorrect description of our TEP theory for the momentum pinch, stating that "Hahm et al. assume mixing of the toroidal angular momentum," while we did not.

II. ON THE SCALING OF THE PINCH TO DIFFUSIVITY RATIO FROM AN-ALYTIC MODELS

We have stated¹ that the $1/L_n$ term in the analytic formula from Ref. 5, i.e., $V_{pinch}/\chi_{\phi} =$ $-1/L_n - 4/R$, cannot be attributed to the Coriolis drift, which vanishes in the limit $1/R \rightarrow 0$. If such a linear dependence on L_n^{-1} is real, it should come from a different physics mechanism. Note that we did not claim that a L_n^{-1} dependence is impossible, in general. The comment by Peeters et al., lists various dimensionless quantities which appear in the linear gyrokinetic equation (including R/L_n), and argues that their pinch to diffusivity ratio formula from a simple fluid theory does not contradict the general properties of the linear gyrokinetic equation. While their result is dimensionally correct, their analytic derivation neglected wave particle resonances including the one involving the magnetic drift, and additionally local toroidicity ($\epsilon = r/R_0$), magnetic shear and geodesic curvature, any relation of their result to the general properties of the gyrokinetic equation in toroidal geometry is already disconnected. Then, what is the origin of that $1/L_n$ dependence in their formula? They used the ion density continuity equation (Eq. (13)), rather than the ion temperature evolution equation (Eq.(15)). Restoring dimensions to various frequencies to make our physical argument clear, their derivation is based on a dominant balance between $(\omega - \omega_{*e})\delta\phi$ and $-2\omega_{di}(\delta T_i + 2\delta\phi)$. The density gradient dependence comes from the $\omega_{*e}\delta\phi$ term. If we take this relation seriously, $\delta\phi$ should be more strongly ballooning at the low field side compared to δT_i , since the magnetic curvature related ω_{di} is the origin of the ballooning structure. Unfortunately this is quite contrary to the results of fully developed ITG turbulence in toroidal geometry which indicate that δT_i balloons more strongly than $\delta \phi$.⁷ This shows that

	Hahm, Diamond, Gurcan	Gurcan et al (PRL 08);	Peeters et al
	and Rewoldt	Hahm et al	(Phys. Rev. Lett. 07)
	(Phys. Plasmas 07)	(Phys. Plasmas 08)	
Starting Eqn.	Gyrokinetic Eqn. in Lab	Local Angular Mom. Density	Gyrokinetic eqn. in Rotating
	(Hahm 88)	Conservation	Frame (Brizard 95)
Effects of Mode Structure	Characterized by $F_{balloon}$;	Characterized by $F_{balloon}$;	Local Analysis
	Calculated by FULL-code		
	for exemplary case		
Instability Considered in	Any long-wavelength	Only mode-independent part	Long-wavelength ITG
Analytic Theory	instabilities on gyroradius	of pinch:	instability with adiabatic
	scale; mode-dependent	Turbulent Equipartition Pinch	electrons
	calculation ends with general	(TEP) has been considered	
	expression which has not		
	been pursued to the end		
Physics Mechanisms for	Magnetic curvature	Homogenization (Mixing)	Coriolis-force-driven drift
Momentum Pinch	modification to parallel	of magnetically-weighted	coupling density, flow, and
	acceleration, leading to	angular momentum density	temperature fluctuations
	B^{\ast} symmetry breaking		
Physics of TEP Pinch	TEP part of pinch identified	Presented starting from local	Not discussed
	from GK derivations,	conservation laws and	
	discussed in the context of	quasilinear theory of	
	homogenization theory	magnetically-weighted	
		angular momentum density	

TABLE I: Comparison of Different Approaches

their simple analytic model has artifacts which should be taken with great caution when it's applied to comparisons to experiments or projection to larger machines. Comparing a numerical result from a linear gyrokinetic calculation with simple analytic formulas in Figure 1, without stating important differences in physical models, assumptions and parameters, is misleading. For instance, they don't specify the equation for "kinetic electrons". Therefore, as presented, it's not even clear what problem has been solved numerically.

Acknowledgments

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