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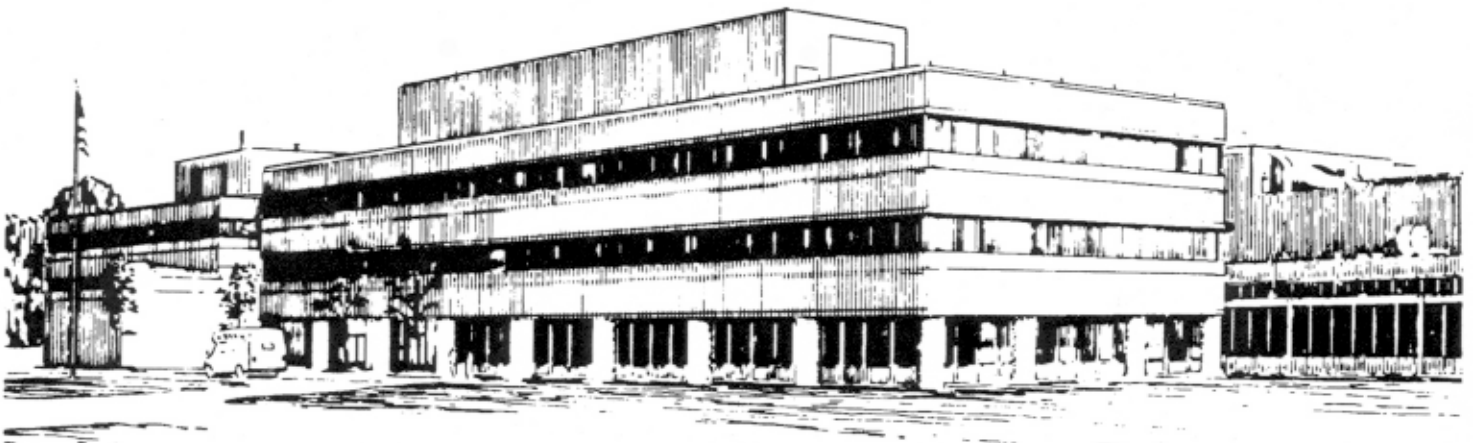
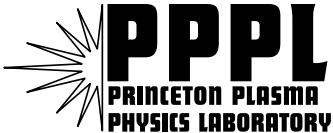
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**Enhanced Mode Conversion of Thermally Emitted Electron
Bernstein Waves (EBW) to Extraordinary Mode**

by

B. Jones, P.C. Efthimion, G. Taylor, T. Munsat, J.R. Wilson, J.C. Hosea,
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**Enhanced Mode Conversion of Thermally Emitted Electron Bernstein Waves (EBW) to
Extraordinary Mode**

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In the CDX-U spherical torus, ~100% conversion of thermal EBWs to X-mode has been observed by controlling the electron density scale length (L_n) in the conversion region with a local limiter outside the last closed flux surface. The radiation temperature profile agrees with Thomson scattering electron temperature data. Results are consistent with theoretical calculations of conversion efficiency using measured L_n . By reciprocity of the conversion process, prospects for efficient coupling in EBW heating and current drive scenarios are strongly supported.

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In many high- β magnetically confined plasmas, standard electron cyclotron emission (ECE) electron temperature (T_e) profile diagnostics, as well as EC heating and current drive, cannot be employed since the electron plasma frequency is much larger than the electron cyclotron

frequency ($f_{pe} \gg f_{ce}$). Fundamental and lower f_{ce} harmonic electromagnetic waves are evanescent in the core of the plasma, and higher harmonics that are accessible do not meet the blackbody emission condition of optical thickness $\tau > 2$. The electron Bernstein wave (EBW) has been proposed as an alternate method for measuring the T_e profile in a high- β plasma. [1,2] Since the EBW is an electrostatic wave it can propagate above the critical density in a magnetized plasma, and is strongly absorbed at the f_{ce} harmonics, with $\tau \approx 300$ in CDX-U. [2,3,4] The EBW can mode-convert to either an O- or X-mode electromagnetic wave at the upper hybrid resonance (UHR) layer. The resulting electromagnetic waves emitted can be measured with an antenna and radiometer as in the standard ECE technique.

Conversion between EBW and O-mode waves via the slow X-mode (B-X-O process) occurs at oblique angles in a narrow range of $n_{||}$ whose optimal value is determined by f_{ce}/f and whose width is generally determined by the electron density scale length (L_n) in the conversion region. [5] This process has been extensively studied in both emission and heating experiments on the W7-AS stellarator, with results in good agreement with theory. [1,6]

EBW conversion to X-mode (B-X process) occurs for $n_{||} \neq 0$ with a mode conversion efficiency (C) sensitively dependent on L_n in the conversion region at the UHR. A 1D slab model results in the analytic theory for $n_{||} \neq 0$ presented in [7]. The full expression for mode conversion efficiency is

$$C = C_{max} \cos^2(\phi/2 + \theta) \quad (1)$$

where $\cos^2(\phi/2 + \theta)$ is a factor relating to the phasing of the waves in the mode conversion region with $\theta = \arg \Gamma(-i\eta/2)$, and ϕ evaluated in the manner of [8] for the case of the high-field cutoff close to resonance. The maximum mode conversion efficiency (C_{max}) is given by

$$C_{max} = 4e^{-\pi\eta}(1 - e^{-\pi\eta}) \quad (2)$$

When the magnetic scale length in the mode conversion region $L_B \gg L_n$ as in CDX-U,

$$\eta \approx (2\pi f_{ce} L_n / (c \alpha)) ((1 + \alpha^2)^{1/2} - 1)^{1/2} \quad (3)$$

where $\alpha = f_{pe}/f_{ce}$ evaluated at the UHR layer. This conversion is expected to be less sensitively dependent on $n_{||}$, and is the process we have studied in CDX-U. It is also being studied on the MST reversed-field pinch. [9]

Obtaining $C \sim 100\%$, or equivalently radiation temperature $T_{rad} \sim T_e$, requires $L_n \approx 0.5$ cm in CDX-U. Optimizing C is also desirable so that power can be effectively coupled to the plasma for EBW heating and current drive. Studying EBW emission evaluates the same mode conversion physics that affects the inverse processes of heating and current drive [10], so this research tests the viability of proposed X-mode EBW current drive schemes. [11,12]

Further distinguishing emission measurements on CDX-U from those performed on other machines is that in an ST, the mode conversion for lower harmonics typically occurs outside the last closed flux surface (LCFS). L_n can be diagnosed by Langmuir probes and modified by material limiters in this region.

Two independently calibrated, fast frequency scanning, heterodyne radiometers measure fundamental (4-8 GHz) and second harmonic (8-12 GHz) EBW emission every 20 μ s. [13] Localization of the EBW emission source to the f_{ce} resonant surfaces has been verified by observing the response of the T_{rad} profile to cooling gas puffs at the plasma edge. [1,14] This justifies a comparison between the measured T_{rad} and Thomson scattering T_e profiles in order to infer a value of C . In previous experiments with an antenna outside a vacuum window on CDX-U, $C \sim 10\%$ was observed. [12] Similar observations have been made on NSTX, resulting in good agreement with theoretical C calculated using $L_n = 1.5$ cm, as measured by Thomson scattering.

[15] However, even with the steep edge density profile provided by an NSTX H-mode, a maximum mode conversion efficiency of only 15% was observed.

Rather than relying on the density profile naturally provided by the plasma, it is necessary to create a shorter L_n at the UHR layer outside the LCFS in order to reach $C \sim 100\%$. To meet this goal, an in-vacuum antenna along with a movable local limiter has been installed in CDX-U, shown in Fig. 1. The quad-ridged horn antenna points perpendicular to the LCFS ($n_{\parallel} \approx 0$) on the outboard midplane, oriented with the edge field line pitch so as to measure predominantly X-mode emission with one set of ridges and O-mode with the other. X-mode T_{rad} 2-3 times greater than O-mode T_{rad} is measured, consistent with the lower sensitivity of the O-mode antenna to rays with $n_{\parallel} \neq 0$. The local limiter shortens L_n in the scrape-off layer (SOL) where the B-X mode conversion occurs for f_{ce} and $2f_{ce}$, thus optimizing C for $\sim 100\%$ conversion. As the conversion occurs outside the LCFS, the local limiter only modifies the density profile in the SOL immediately in front of the antenna and is not the primary limiter for the plasma.

Also shown in Fig. 1, an array of Langmuir probes adjacent to the antenna measures the density profile in the mode conversion region so that the observed emission can be compared to C calculated using L_n measurements. These 5 mm long cylindrical probes can be swept in voltage to measure T_e or biased negatively to measure ion saturation current (I_{sat}) from which electron density (n_e) can be calculated.

Figure 2 (a) shows the significant steepening of L_n outside the LCFS due to the local limiter. For each point, data were averaged for approximately five shots with similar plasma parameters. I_{sat} was averaged over 0.1 ms during each shot in order to smooth out fluctuations. The profile naturally occurring in the SOL with $L_n = 3-6$ cm (diamonds, dashed line) was measured by scanning the entire assembly, using the furthest inboard tip which is unperturbed by the local

limiter. With the local limiter located near the LCFS and measuring n_e with the probe tips outboard of the limiter (triangles), an average density scale length $L_n=0.66\pm 0.07$ cm was measured (solid line is a best fit to three points). As will be discussed, this value is consistent with $\sim 100\%$ B-X conversion efficiency.

Using these density profiles, the UHR frequency $f_{UH}=(f_{pe}^2+f_{ce}^2)^{1/2}$ is calculated as a function of major radius in Fig. 2 (b). f_{ce} is calculated using $|B|$ from the equilibrium code JSOLVER constrained to the measured toroidal plasma current (60 kA). [16] Since $B_p \ll B_t$ in CDX-U, JSOLVER is expected to provide a reasonable estimate of $|B|$. An EBW of a given frequency mode-converts when the outgoing wave reaches the radial position at which $f=f_{UH}$. f_{UH} calculated using the natural SOL n_e profile (dashed line) illustrates that in CDX-U, the fundamental and second harmonic EBW mode conversion naturally occurs in the SOL, near the vessel wall at $R=70$ cm in the case of the 4-8 GHz fundamental emission. With the local limiter present (solid line), the mode conversion for 4-12 GHz occurs in a few-centimeter-wide UHR layer between the limiter and antenna position where L_n is shortened.

The effect of the local limiter on the EBW emission is seen in Fig. 3. With the antenna and local limiter retracted near the vessel wall so that the mode conversion occurs in a region with long L_n , the fundamental emission is observed at a low level (triangles). With the local limiter near the LCFS so that the mode conversion occurs in a region of short L_n , we see the emission increase by an order of magnitude (diamonds, solid line). We also plot the second harmonic T_{rad} (diamonds, dashed line), and note that there is favorable agreement with Thomson scattering T_e data (squares) for both fundamental and second harmonic mode-converted EBW emission with L_n shortened by the local limiter. The hollow temperature profile is typical, and is expected as CDX-U is a short-pulse machine with a plasma duration of ~ 15 ms. Only a 30% reduction in

second harmonic T_{rad} is seen without the local limiter, likely due to the natural steepening of L_n near the LCFS seen in Fig. 2.

The EBW T_{rad} points were mapped from radiometer frequency to R , with error bars reflecting the frequency resolution of the radiometers shown on selected points. 15% T_{rad} error bars are due to systematic error in the absolute calibration, performed using Dicke-switching of a blackbody source. [17] Data points obscured by cyclotron harmonic overlap or for which the mode conversion region is perturbed by the presence of the antenna are not shown.

The Thomson scattering measurements are taken along a vertical axis (z) at a fixed beam radial position. Plotted in Fig. 3 is the average of two data sets for similar CDX-U discharges measured at the start of the time window in Fig. 4. T_e for each set results from a fit to scattered spectra integrated over 16-48 shots to resolve low photon statistics. Mapping from z to R is performed using canonical CDX-U flux surface shapes. Error bars in R are calculated by perturbing the location of the magnetic axis and the plasma elongation. The mapping of the points to outboard radial positions far from the Thomson laser location is especially sensitive to the shape of the flux surfaces, resulting in larger error bars in R . Points closer to the center of the plasma are not available because the laser beam does not pass through the magnetic axis.

Large fluctuations in the emission signal are observed, which we interpret as being due to variation in L_n resulting from density fluctuations at the local limiter. These fluctuations can be seen in the time evolution of T_{rad} and I_{sat} shown in Fig. 4. The T_{rad} profiles shown in Fig. 3 represent single radiometer sweeps selected at the peak of fluctuating emission within the analysis time window. Vertical arrowed lines show the peak-to-peak fluctuation at 6 GHz and 10 GHz. Note that the fluctuation is greater at 6 GHz, extending down to about 10% of the peak signal, while the 10 GHz fluctuation drops to only about 40% of the maximum T_e .

The n_e profile data from the probes and the EBW emission measurements can test the theory of B-X mode conversion presented in [7]. Fig. 5 (c) shows theoretical mode conversion efficiency C calculated from equation (1) as a function of L_n at both 6 and 10 GHz (fundamental and second harmonic emission frequencies). The average L_n measured behind the local limiter is shown (dashed vertical line), with the shaded region representing the error bars. It is seen that $C \sim 100\%$ is theoretically attainable with the short L_n produced by the local limiter, consistent with the comparison between T_{rad} and Thomson T_e profiles. Interpreting the fluctuating emission observed as being due to fluctuations carrying L_n out to near 2 cm (dotted line), we see that the theoretical C drops to 10% for the 6 GHz case and 40% for 10 GHz. This is consistent with the observed fluctuation in the emission signal, as shown in Fig. 3, and with the 0.4 and 3.4 cm worst-case limits on L_n obtained by considering the ranges of fluctuating n_e measured at the probe locations spanning the conversion layer. Note that had we neglected the phase factor and calculated only C_{max} versus L_n (Fig. 5 (a)), we would not have predicted the differing levels of T_{rad} fluctuation observed. It is the frequency dependence in $\cos^2(\phi/2+\theta)$ near $L_n \sim 2$ cm (Fig. 5 (b)) that leads to this difference in C at 6 and 10 GHz.

Further evidence that fluctuating L_n is playing a role in modifying C , leading to fluctuating emission, is seen by comparing the T_{rad} and probe I_{sat} time evolution. For several probe tip positions, the cross-correlation between these signals was calculated in a time window approximately 1 ms wide. 70% anti-correlation was observed for the probe located 0.6 cm behind the local limiter and emission at 5.5 GHz, which mode-converts near the probe location. The emission peaked when the density behind the limiter dropped, consistent with L_n shortening. Correlation was not seen for probes 2 cm on either side of this location.

100% B-X mode conversion efficiency has been observed in CDX-U by controlling L_n at the UHR layer, allowing direct measurement of the T_e profile from mode-converted EBW emission. The measured T_e profile was similar to that measured by Thomson scattering. $C \sim 100\%$ and measured L_n at the UHR are consistent with the theory of [7]. The $\cos^2(\phi/2+\theta)$ phase factor in this theory has been found to be important, and explains the frequency dependence of the observed T_{rad} fluctuations. Since the mode conversion occurs in the SOL for an ST, L_n can be controlled and optimized with a local limiter that does not perturb the plasma. Similarly, reciprocity of the mode conversion process is a strong justification for using a local limiter with an X-mode electromagnetic heating or current drive antenna to achieve efficient coupling to the EBW branch.

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FIG. 1. The CDX-U EBW diagnostic combines a quad-ridged horn antenna to measure emission, a movable local limiter (half shown) to modify L_n in front of the antenna to optimize mode conversion, and a Langmuir probe array to measure L_n .

FIG. 2. (a) The $L_n=3-6$ cm electron density profile naturally occurring in the SOL (diamonds, dashed line) and the $L_n=0.66-0.07$ cm profile created by the local limiter (triangles, solid line). (b) The corresponding UHR frequency profiles, determining the mode conversion location for a wave of frequency $f = f_{UH}$. The local limiter creates a narrow mode conversion layer in front of the antenna for the fundamental and second harmonic EBW frequency ranges (shown shaded).

FIG. 3. The radiation temperature without the local limiter (triangles). With the local limiter, the peak fundamental emission (diamonds, solid line) and second harmonic emission (diamonds, dashed line) together map out the T_e profile and are consistent with T_e measured by Thomson scattering (squares). The emission fluctuation levels at 6 and 10 GHz are indicated by vertical arrowed lines.

FIG. 4. Time evolution of a typical CDX-U discharge. (a) Toroidal plasma current, (b) line-averaged density ($R=35$ cm), (c) ion saturation current from Langmuir probes showing edge n_e fluctuation (local limiter at $R=56.6$ cm, data from two separate shots), and (d) EBW T_{rad} at 10 GHz, showing multiple peaks resulting from gas puff modulation and fluctuation resulting from changing L_n . Analysis was performed in the shaded time window.

FIG. 5. (a) The maximum mode conversion efficiency C_{max} for 6 GHz (solid) and 10 GHz (dashed) emission as a function of L_n just outside the CDX-U LCFS, (b) the $\cos^2(\phi/2+\theta)$ phase factor, and (c) the theoretical mode conversion efficiency $C=C_{max}\cos^2(\phi/2+\theta)$.

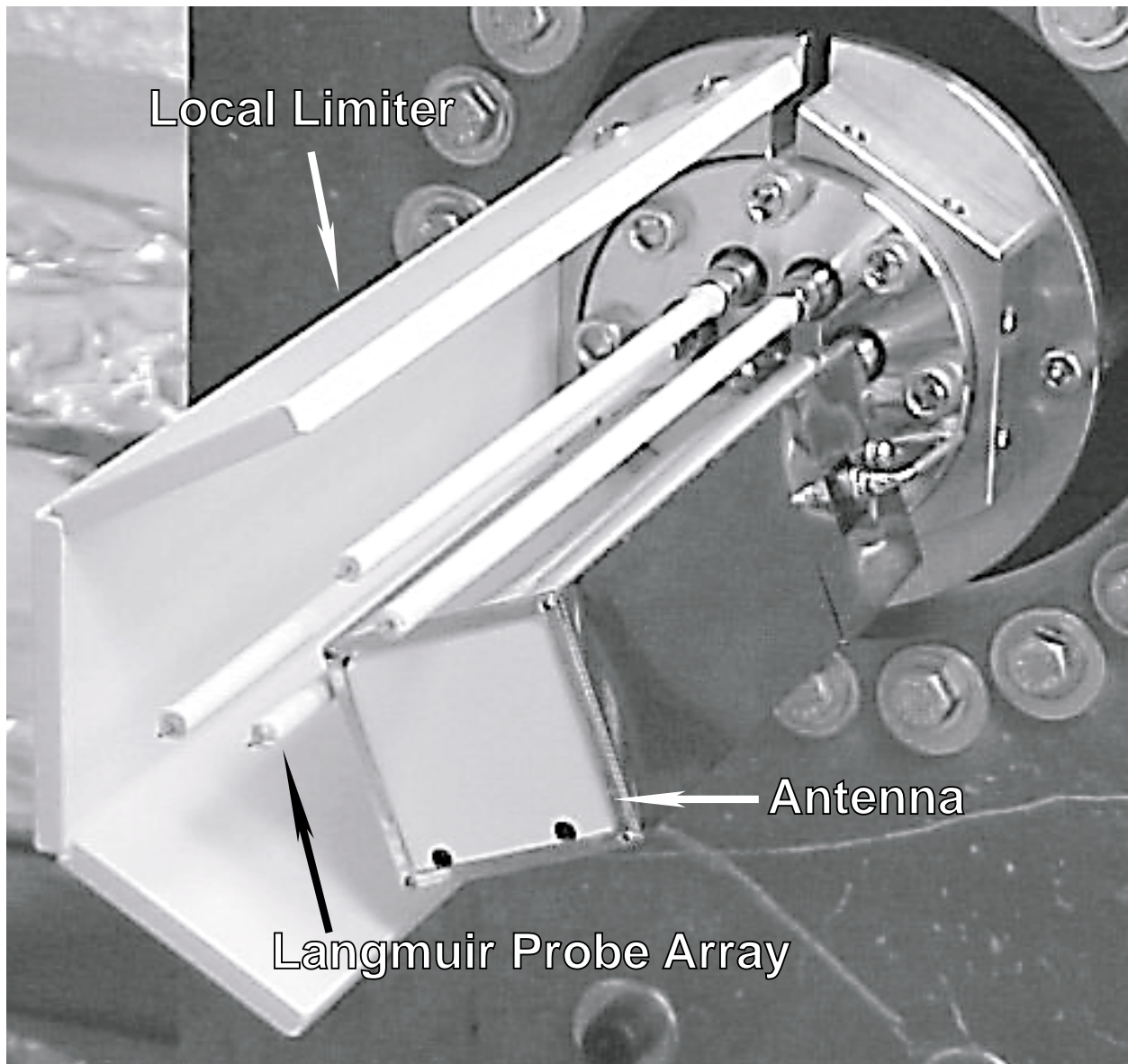


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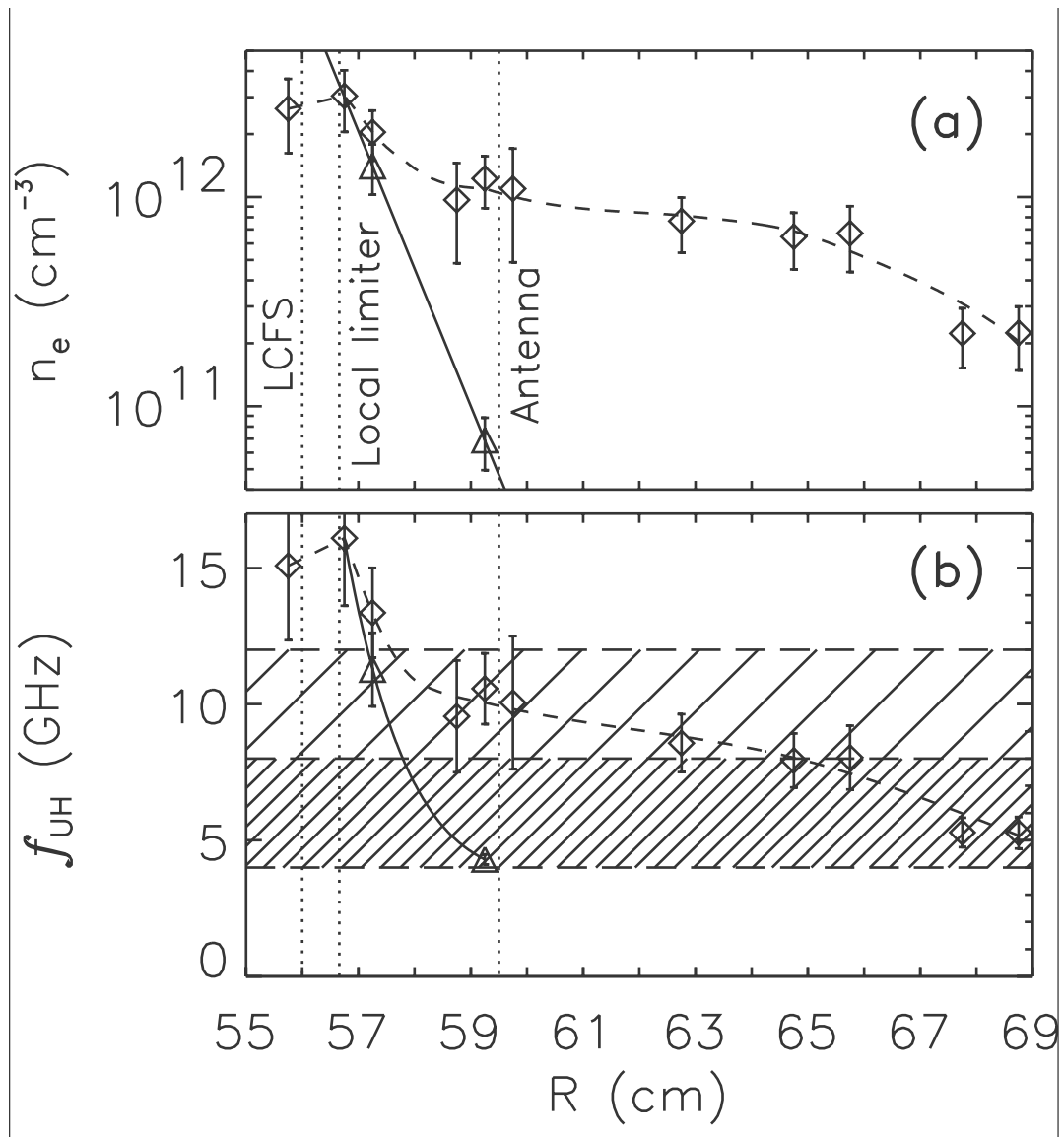


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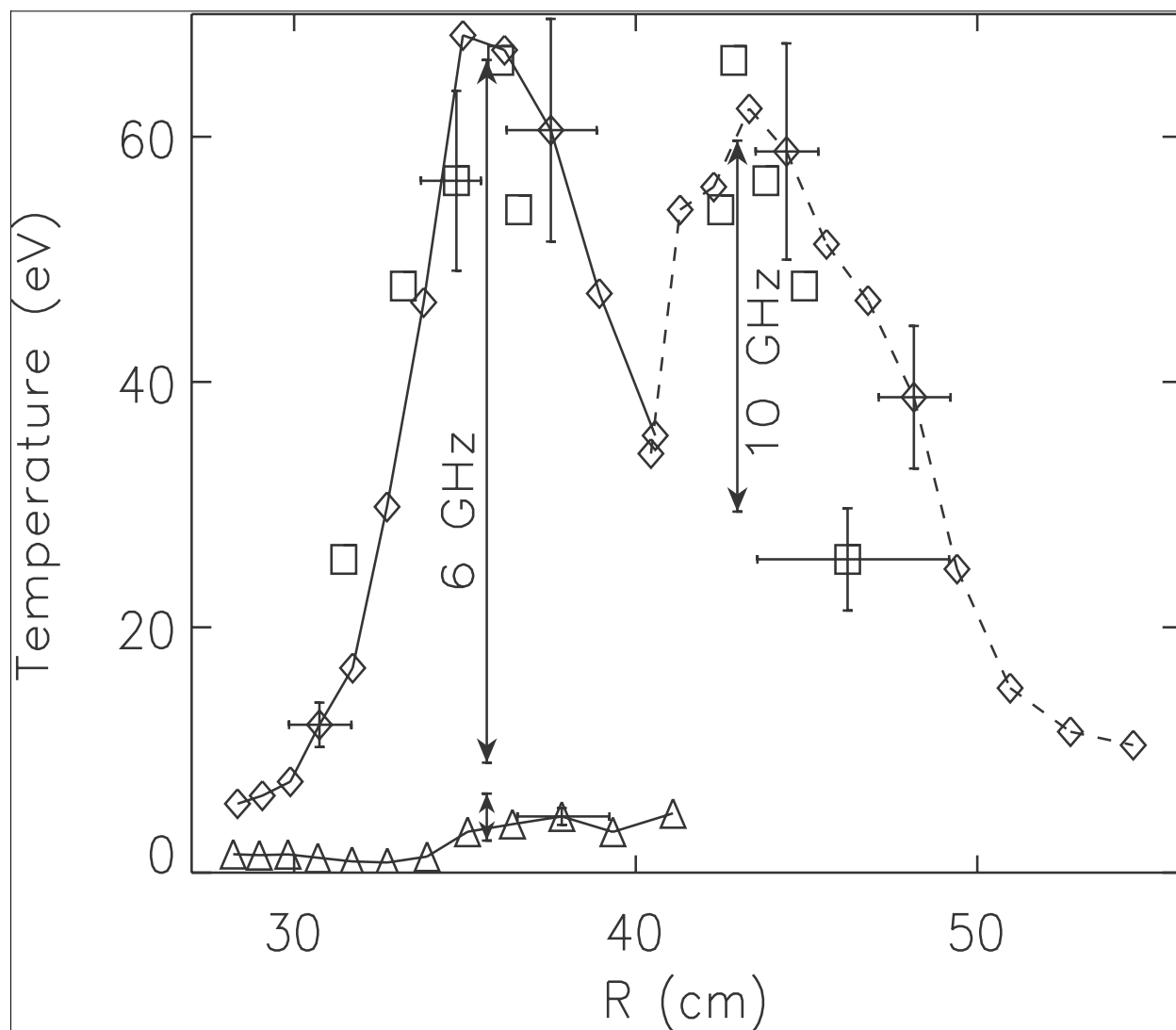


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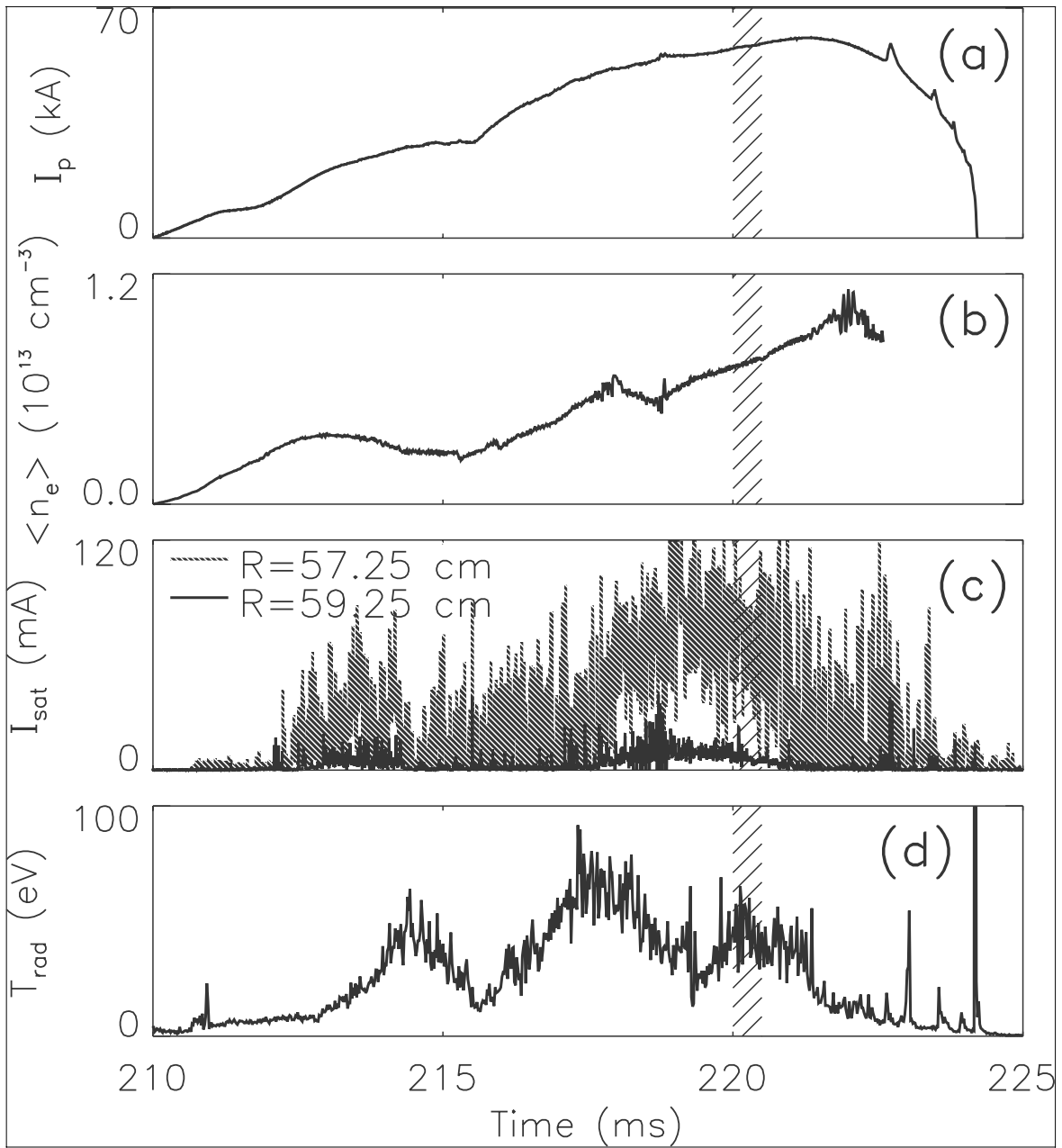


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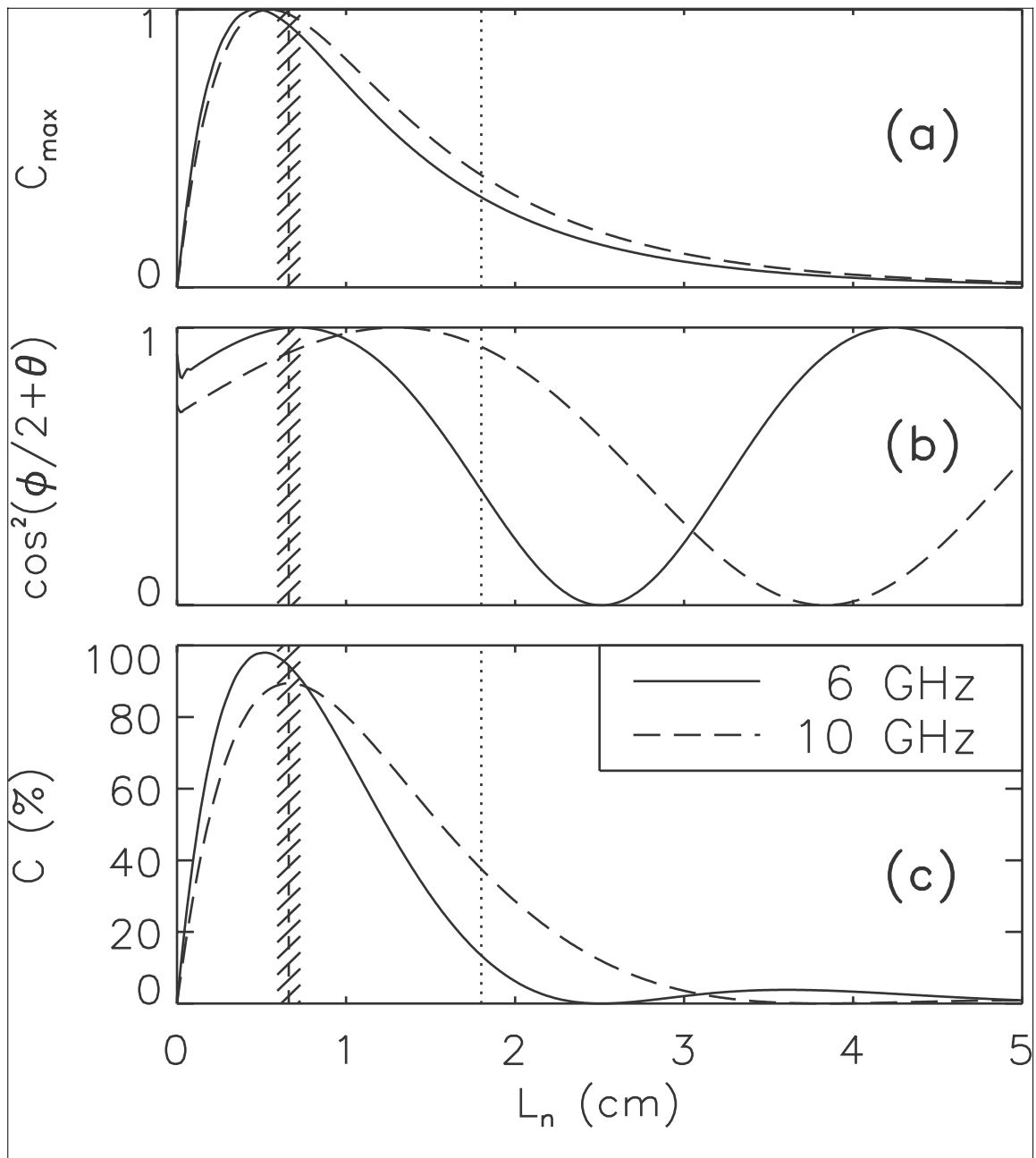


FIGURE 5, B. Jones, Phys. Rev. Lett.

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