The Roles of Electric Field Shear and Shafranov Shift in Sustaining High Confinement in Enhanced Reversed Shear Plasmas on the TFTR Tokamak


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The relaxation of core transport barriers in TFTR Enhanced Reversed Shear plasmas has been studied by varying the radial electric field using different applied torques from neutral beam injection. Transport rates and fluctuations remain low over a wide range of radial electric field shear, but increase when the local ExB shearing rates are driven below a threshold comparable to the fastest linear growth rates of the dominant instabilities. Shafranov-shift-induced stabilization alone is not able to sustain enhanced confinement.

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The possible role of the radial electric field in forming and sustaining transport barriers in H modes and VH modes has been discussed extensively.\textsuperscript{1,2,3,4} TFTR Enhanced Reversed Shear (ERS)\textsuperscript{5} and DIII-D Negative Central Shear (NCS)\textsuperscript{6} plasmas possess transport barriers deep in the plasma core, and large values of the radial electric field $E_r$ and its gradient have been associated with high confinement in these regimes.\textsuperscript{7,8} However, it remains an open question whether $E_r$ plays a causative role in reducing transport in these cases. Indeed, high core particle, energy, and momentum confinement obtained by any means will lead to increased pressures and velocities, and most likely to large values of $E_r$ and $\nabla E_r$.

While $E_r$ plays a central role in proposed mechanisms for transport bifurcation and good confinement,\textsuperscript{9} other proposals have been made in which it is not involved.\textsuperscript{10,11} The suggestion that $E_r$ is key in balanced-injection TFTR ERS plasmas takes the following form: central fueling and heating results in steep gradients in the plasma pressure $p$, which yield large gradients in $E_r$ and the $E \times B$ flow shear.\textsuperscript{12,13} With sufficiently large flow shear, turbulence is decorrelated. This leads to a reduction in transport, and to a further increase in $\nabla p$ and confinement. Low current density yields a large Shafranov shift $\Delta$, and thus increased $\nabla p$ and $E \times B$ shear, as compared to plasmas with peaked current density profiles of the same stored energy. The alternative explanation for the formation of core transport barriers relies on the role of $\Delta$ itself. In Ref. 10, reduction of instability drives and the formation and sustainment of transport barriers is predicted for TFTR reversed shear plasmas as a result of favorable precession of barely trapped particles induced by large gradients in the Shafranov shift $\Delta'$. Similar arguments were made examining ballooning-type instabilities in the plasma edge.\textsuperscript{11} Proposals based on both $E \times B$ and $\Delta'$ effects suggest a combined picture in which growth rate reduction induced by large $\Delta'$ enables the $E \times B$ shear to be effective. In all of the above scenarios, good confinement is expected to be reinforced by the stabilization of ion-thermal-gradient turbulence from the peaking of the density profile.\textsuperscript{14}

Results presented in this Letter indicate that $E \times B$ shear effects are necessary, and that Shafranov shift effects are not sufficient, to maintain the observed low radial transport and fluctuation levels in ERS plasmas. Experimentally, it is difficult to separate the roles of $E \times B$ shear and $\Delta'$ effects. Since steep plasma pressure gradients $\nabla p$ and large values of $E_r$ accompany large
Shafranov shifts, a means of varying $E_r$ independent of $\nabla p$ is required to decouple the two effects. In these experiments, ERS plasmas were generated with similar neutral beam powers and heating profiles, which fixed quantities central to $\Delta'$-induced stabilization. However, these plasmas had different applied torques and thus varying degrees of toroidal velocity $V_\phi$. For any plasma species, the radial force balance equation is given by $E_r = \nabla p/(nZe) + V_\theta B_\theta - V_\phi B_\phi$, where $n$ is the density of the species in question, $Z$ is the charge number, $e$ is the electronic charge, $V_\theta$ is the poloidal rotation velocity, $B_\theta$ is the poloidal magnetic field, and $B_\phi$ is the toroidal field. Thus $V_\phi$ variations result in changes in $E_r$ and its shear. The causative role of $E_r$ in sustaining enhanced confinement is in part indicated by the observation that core fluctuation and transport levels increase when the $E\times B$ shear is driven below a critical level, but remain low and unchanged above that threshold. This threshold behavior is anticipated in the work of Ref. 12. Variations of amplitude and sign of $V_\phi$ also enable tests of the role of rotation, together with $\nabla p$, in determining $E_r$'s influence on enhanced core confinement, and allow $E_r$ to be altered without introducing toroidal asymmetries in the magnetic geometry.

Plasmas with reverse magnetic shear were generated in the standard way by heating them with modest neutral beam power (7 MW) during the period of current ramp-up. Transitions to the ERS regime were obtained during a 350 ms period of high-power beam heating (28 MW) in a balanced configuration having nearly equal power injected tangentially parallel (co) and antiparallel (counter) to the plasma current. During this period the central electron density increased rapidly due to strong core particle fueling and improved core particle confinement, reaching $\sim 9 \times 10^{19}$ m$^{-3}$ (Fig. 1). Favorable ERS confinement was sustained for variable durations in the subsequent "postlude" period of lower-power heating (14 MW), as indicated by the continued rise in central electron density. Six neutral beam sources were used in different combinations during the postlude phase, ranging from pure co-injection to predominantly counter-injection. This procedure varied the rotation speed, and thereby the $E\times B$ shear, while maintaining a constant Shafranov shift.

The plasma pressure and pressure peakedness, total particle number, stored energy, $\Delta'$, and global energy confinement time remained nearly constant throughout the postlude period so long as the discharges remained in the ERS regime. Eventually, however, the core transport barrier
was lost in some of the plasmas; they suffered a back-transition to poorer confinement, indicated most simply by the decay in central electron density. There is a clear correlation between the applied beam torque and occurrence of such a back-transition (Fig. 1). Counter-dominated, balanced, and slightly co-dominated injection sustained ERS confinement until the end of beam injection, but predominantly co-dominated injection reproducibly triggered a back-transitions. Pure co-injection yielded the earliest confinement losses. Following back-transitions, the electron particle diffusivity $D_e$ increased by more than an order of magnitude in the region of previously-good confinement, and the electron density collapsed (Fig. 2). $D_e$ was determined by a calculation of the particle source and electron flux $\Gamma_e$ in the TRANSP code$^{16}$ and is defined by $\Gamma_e \equiv -D_e \nabla n_e + V_{\text{ware}}$, where $V_{\text{ware}}$ is the Ware pinch. The ion thermal diffusivity (not shown) also increased in the core region following the back transition.

The correlation of back-transitions with varied applied torques at constant plasma pressure suggests that reductions in $E \times B$ shear are involved in the loss in ERS confinement. In a toroidal geometry, the gradient in the quantity $E_r/R B_\theta$ characterizes the decorrelation of turbulence, where $R$ is the major radius. On the outer midplane, a characteristic rate for shearing turbulence can be written as $\gamma_{E \times B} = E_r/B \left[ 1/E_r \partial E_r/\partial R - 1/B_\theta \partial B_\theta/\partial R - 1/R \right]$, where $B$ is the total magnetic field magnitude. In determining $E_r$, $B_\theta$ was measured with the Motional Stark Effect$^{17}$ diagnostic in the first 1.9 s of injection, when contributions from the plasma $E_r$ to the total electric field experienced by the beam neutrals were small.$^{18}$ After this time, TRANSP calculations were used to obtain $B_\theta$. $V_\phi$ and the carbon pressure $p_c$ were measured with charge exchange recombination spectroscopy,$^{19}$ and $V_\theta$ was calculated with the NCLASS code using the neoclassical treatment of Hirshman and Sigmar.$^{20}$ In general, the $V_\phi B_\theta$ term subtracts from the $\nabla p_c$ and the $V_\theta B_\phi$ terms in the carbon force balance. Thus, increasing $V_\phi$ in the co-injection direction after the balanced phase leads to a reduction in $E_r$ and its gradient. Profiles of $E_r$ and its components from the carbon force balance equation are shown in Fig. 3 for a co-rotating plasma at two times. The first time is shortly after the 28 MW balanced phase, and the second is in the earliest stages of the back-transition. The local electron density and pressure gradients at the latter time have just begun to fall. The $\nabla p_c$ and $V_\theta B_\phi$ contributions to $E_r$ are similar between these two times, but as a result of the increasing $V_\phi$, the
magnitude of $E_r$ drops by a factor of three at $r/a = 0.3$. At that point, $V_\theta$ increased from -$0.3 \times 10^5$ at 2.3 s to $1.5 \times 10^5$ m/s at 2.5 s. The $V_\theta B_\theta$ term shown in Fig. 3 is negative in the outer half of the plasma as a result of the measured counter-rotation that is present even with co-dominated injected power. NCLASS calculations indicate that the working ion $V_\phi$ is also counter-directed in the outer half of the plasma. TRANSP analysis shows that this is consistent with the presence of a counter-directed torque, established by a radial current of thermal particles that arises to preserve ambipolarity in response to ripple loss of about 10% of the beam ions. Regarding $V_\theta$, measured differences in $E_r$ in supershots with different applied torques are consistent with $V_\theta$ being driven primarily by neoclassical processes included in NCLASS, including strong poloidal damping. However, large pressure gradients raise concern regarding violation of the usual size ordering assumed in neoclassical theory. Because the trapped orbit widths of carbon ions are small compared to the electric field and pressure gradient scale lengths, this ordering is not violated for this impurity. The pressure gradient scale length $\lambda_p$ is 10 - 20 times the trapped carbon orbit size $\lambda_c$ for $r/a > 0.2$, without considering the influence of orbit squeezing. Squeezing effects reduce the orbit size by roughly 50% for $r/a < 0.2$, leading to $\lambda_p/\lambda_c > 10$ for all radii. Orbit squeezing is included in the NCLASS calculations using an approximate method. Since large values of $dE_r/dr$ change the carbon ion collisionality [Ref. 22], the predictions of $V_\theta$ and thus $E_r$ are modified somewhat for $r/a < 0.25$ (Fig. 3). Such physics issues surrounding the $V_\theta$ evaluation have motivated the development of a diagnostic aimed at measuring this quantity directly.

The pressure remains peaked in the region where the maximum linear growth rate $\gamma_{\text{lin}}^{\text{max}} < \gamma_{E \times B}$ (Fig. 4). The pressure collapses when $\gamma_{E \times B}^{\text{max}}$ is driven by rotation below a critical value comparable to $\gamma_{\text{lin}}^{\text{max}}$ in the core, indicating that $E \times B$ shear is necessary to sustain enhanced confinement. $\gamma_{\text{lin}}^{\text{max}}$ was calculated with a gyrofluid treatment that includes the role of $\Delta'$, but excludes the effects of $E \times B$ shear. In these plasmas, modes are expected to become unstable primarily by the trapped electron precession resonance. In the co-dominated postlude plasmas, the loss of core stored energy occurs at different times but at comparable values of $\gamma_{E \times B}^{\text{max}}$, again indicating that $E \times B$ shear is necessary to maintain low transport (Fig. 5). The causative role of
E×B shear is further emphasized by the fact that reductions in $\gamma_{\text{E×B}}$ clearly precede back-transitions, while all other plasma quantities, including $\Delta'$, are constant or nearly constant.

Increases in core local fluctuation levels, measured from reflectometry, are correlated with increases in local transport coefficients in plasmas with back-transitions (Fig. 6). In addition, transport coefficients and fluctuation levels remain low until $\gamma_{\text{E×B}}$ falls below a critical value that is comparable to the local value of $\gamma_{\text{lin}}^{\max}$. The insensitivity of transport and fluctuations to variations in $\gamma_{\text{E×B}}$ above a threshold value, and the similar magnitude of $\gamma_{\text{E×B}}$ and $\gamma_{\text{lin}}^{\max}$ at the onset of increased transport and fluctuations is consistent with expectations from Ref. 12. There, nonlinear simulations of ion drift-wave-type turbulence indicate that suppression of turbulence-induced transport should be complete when $\gamma_{\text{E×B}} \sim \gamma_{\text{lin}}^{\max}$. While the fact that $\gamma_{\text{lin}}^{\max} / \gamma_{\text{E×B}} \sim 1/2 - 1$ at the onset of turbulence is suggestive, the more important point is that the predicted threshold character of turbulence suppression is observed. In fact, variations with plasma condition in $\gamma_{\text{lin}}^{\max} / \gamma_{\text{E×B}}$ at the onset of suppression are found in both experiments and simulations. It was suggested in Ref. 12 that parametric dependencies may influence the value of $\gamma_{\text{lin}}^{\max} / \gamma_{\text{E×B}}$ at that time. There, variations of a factor of two in this ratio were observed. Changes in $\gamma_{\text{lin}}^{\max} / \gamma_{\text{E×B}}$ at the start of enhanced confinement of more than a factor of two were also observed in recent ERS experiments in which the toroidal field was varied. Finally, equating $\gamma_{\text{lin}}^{\max}$ with the natural turbulence decorrelation rate is an approximation. The latter is the quantity more appropriately compared to the shearing rate, but it is not readily evaluated. These observations point to the need for study with respect to the identification of the most relevant shear suppression criterion and its underlying dependencies.

The fluctuation amplitude increases gradually as $|\gamma_{\text{E×B}}|$ decreases, suggesting that the smaller values of $|\gamma_{\text{E×B}}|$ are effective in suppressing the turbulence at least partially. Note also that when transport coefficients are near a maximum, $|\gamma_{\text{E×B}}|$ is near its local minimum value. For the plasma with co-only injection in the postlude (Fig 6(a)), transport coefficients and fluctuation levels begin to fall again after 2.6 s. After this time, the $\gamma_{\text{E×B}}$ profile broadens and becomes dominated by gradients in $V_\phi$ rather than $V_p$, indicating that E×B shear from rotation drive may be reducing turbulence, as has been suggested for DIII-D NCS and VH-mode plasmas.
Without consideration of $E \times B$ shear, the fact that back-transitions occur in plasmas with heating, pressure, and $\Delta'$ profiles that are similar until the back-transition to those of plasmas without back-transitions indicates that $\Delta'$ effects alone are not sufficient to maintain enhanced confinement. Gyrokinetic simulations\textsuperscript{26} indicate that the velocity shears in these plasmas are far below those required to excite rotationally driven instabilities\textsuperscript{27,28} which might cause a loss in confinement. They also indicate that stabilizing influences of $V_\phi$ shear are not significant here.

While $\Delta'$ is not sufficient to maintain reduced transport in the absence of $E \times B$ shear, it may still be necessary. $E \times B$ shear suppression may benefit from the reduced growth rates that result from $\Delta'$ effects. Growth rates calculated including $\Delta'$ effects are a factor of two smaller than those obtained excluding these effects. However, the gradual increase of fluctuations and transport with decreasing $|\gamma_{E \times B}|$ indicates that some reductions in transport might be expected for plasmas in which $|\gamma_{E \times B}|$ is large but where growth rates have not had the benefit of significant $\Delta'$-induced reduction. As a result, the steep pressure gradients in TFTR supershots and accompanying large gradients in $E_r$ may produce some reduction in turbulence-driven transport.\textsuperscript{29,30} Differences in $E \times B$ shear from different degrees of $V_\phi$ may explain also many trends in isotope scaling studies, even in L mode, on TFTR.\textsuperscript{31}

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Figure captions

Fig. 1  The central electron density time evolution. Curves are labeled according to the difference on co- vs. counter-injected power, $P_{co} - P_{ctr}$, divided by the total injected power $P_{tot}$. The shaded region indicates schematically the neutral beam heating waveform. The plasmas studied had a major radius of 2.60 m, a minor radius of 0.95 m, a toroidal magnetic field of 4.6 T, and a maximum plasma current of 1.6 MA.

Fig. 2  (a) Profiles of the electron density at four times for a plasma that is co-dominated in the postlude $[(P_{co} - P_{ctr})/P_{tot} = 0.62]$. (b) Radial profiles of $D_e$ for the same plasma. Profiles of $D_e$ for the other plasmas during the ERS period are similar to the profiles shown for 2.3 - 2.4 s.

Fig. 3  (a) Radial profile of $E_r$ for the plasma discussed in Fig. 2 $[(P_{co} - P_{ctr})/P_{tot} = 0.62]$, and the contributions from the components of the carbon force balance equation at 2.3 s. The shaded regions represent the difference in the $V_\theta$ term and the net $E_r$ calculated if orbit squeezing effects are ignored. (b) Same as (a), but for 2.5 s, in the early stages of confinement loss.

Fig. 4  Profiles of shearing rate and total plasma pressure for a counter-dominated plasma $[(P_{co} - P_{ctr})/P_{tot} = -0.4]$ (a,b), and one of the co-dominated plasmas $[(P_{co} - P_{ctr})/P_{tot} = 0.62]$ (c,d). In the co-dominated case, the plasma pressure is unchanged until $\gamma_{ExB}$ falls well below $\gamma_{lin}^{max}$.

Fig. 5  (a) The stored energy, integrated out to $r/a = 0.3$ for plasmas with and without back transitions. This location is near the radius of maximum $\gamma_{ExB}$ before the back-transition, and is near the boundary of the region of low fluctuations (Ref. 8). (b) $\gamma_{ExB}$ at $r/a = 0.3$. Also shown is the linear growth rate $\gamma_{lin}^{max}$ for the co-dominated case with the latest back-transition $[(P_{co} - P_{ctr})/P_{tot} = 0.62]$. Growth rates for the other plasmas during their 14 MW postlude ERS phases are comparable. (c) The gradient in the Shafranov shift, $\Delta'$, at $r/a= 0.3$. 
Fig. 6  The effective particle diffusivity $D_e$, and measured fluctuation amplitudes at $r/a = 0.3$ for plasmas with (a) all co-injection $[(P_{co} - P_{ctr})/P_{tot} = 1.0]$ , (b) predominantly co-injection $[(P_{co} - P_{ctr})/P_{tot} = 0.62]$, and (c) balanced injection $[(P_{co} - P_{ctr})/P_{tot} = 0.0]$ in the postlude.
Figure 1
Figure 2

(a) \( \frac{P_{\text{co}} - P_{\text{ctr}}}{P_{\text{tot}}} = 0.62 \)

(b) \( D_e \)
Figure 3

\( V_\phi \)

\( V_\theta \)

\( \nabla p \)

\( E_r \)

\( (P_{co} - P_{ctr}) / P_{tot} = 0.62 \)

2.50 s

2.30 s
Figure 4
Figure 5
Effective diffusivity ($m^2/s$)

$$D_e$$

$$(P_{co}-P_{ctr})/P_{tot} = 1.0$$

$(P_{co}-P_{ctr})/P_{tot} = 0.62$  

$$(P_{co}-P_{ctr})/P_{tot} = 0.0$$  

$r/a = 0.3$

Figure 6